



LUND
UNIVERSITY

GAS TURBINES – SOME THOUGHTS...

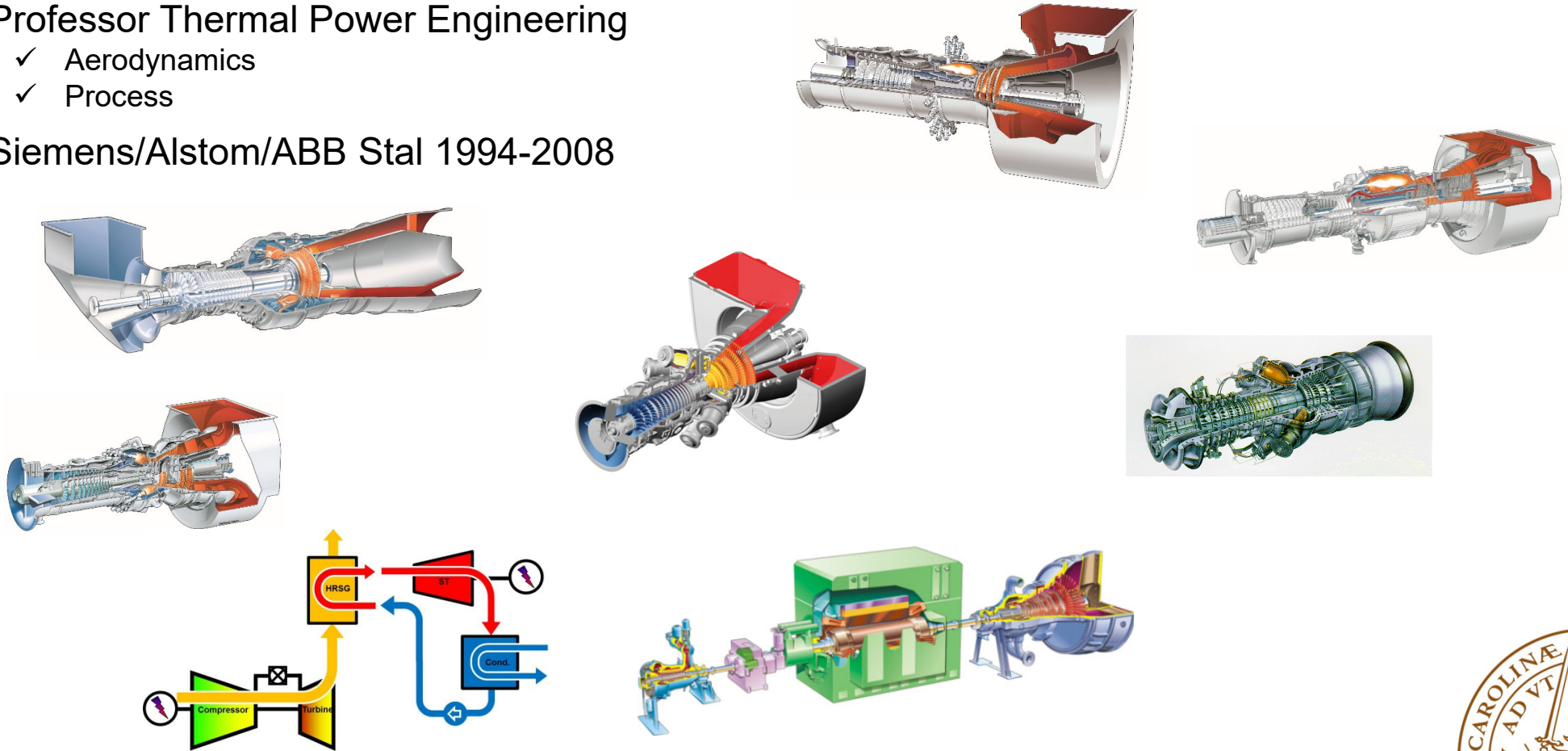
MAGNUS GENRUP, ENERGY SCIENCES



Magnus Genrup, PhD



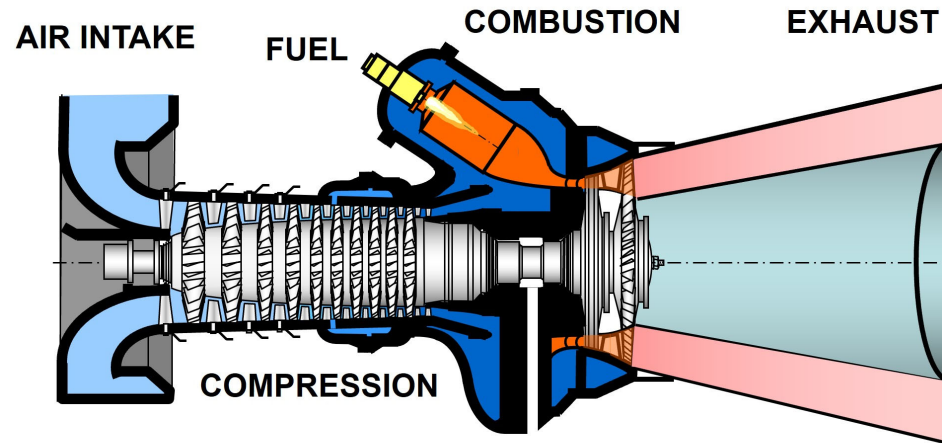
- Professor Thermal Power Engineering
 - ✓ Aerodynamics
 - ✓ Process
- Siemens/Alstom/ABB Stal 1994-2008



Gas turbine vs. reciprocating...



Continuous

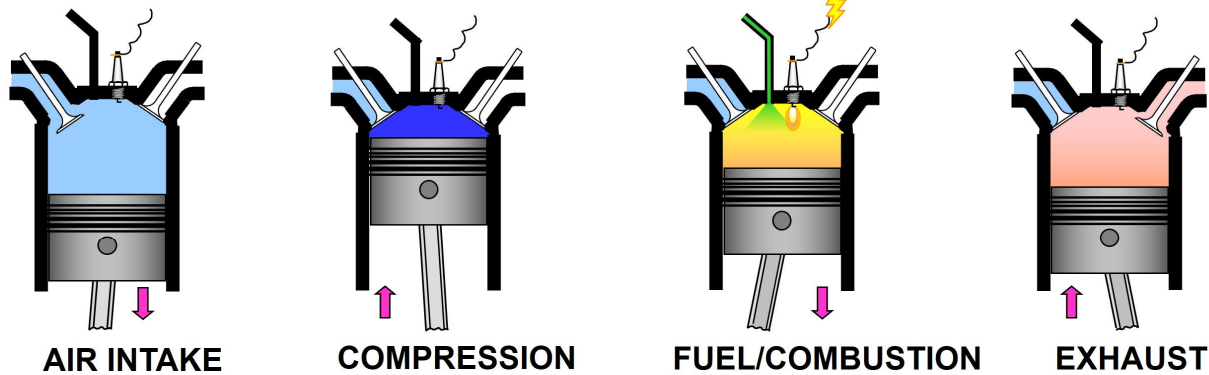


George Brayton
1830-1892



James Joule
1818-1889

Intermittent



Swallowing capacity of turbomachinery

Gas turbine vs. turbocharged IC

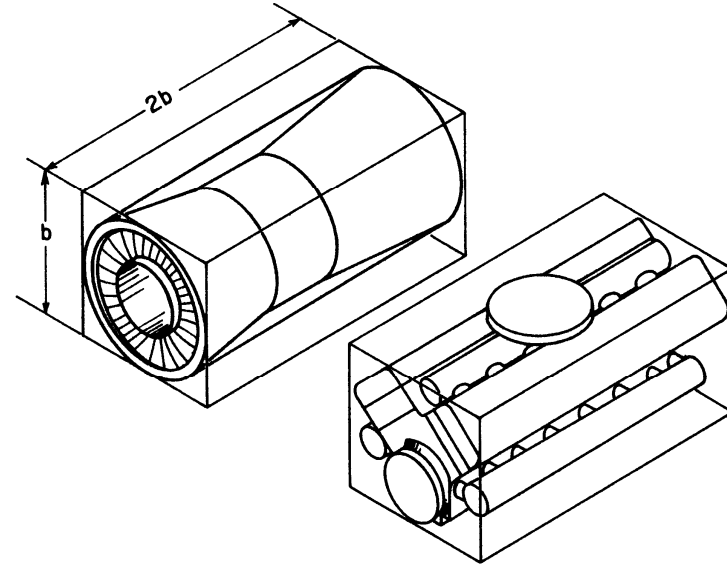


Inlet volumetric flow can be expressed as:

$$\dot{V}_{GT} = \frac{\pi}{4} (0.9b)^2 (1 - 0.5^2) 0.7a = 0.334 ab^2$$

$$\dot{V}_{ICE} = \frac{\pi}{4} (0.2b)^2 0.8a = 0.025 ab^2$$

$$\frac{\dot{V}_{GT}}{\dot{V}_{ICE}} = \frac{0.334 ab^2}{0.025 ab^2} \approx 13.4$$

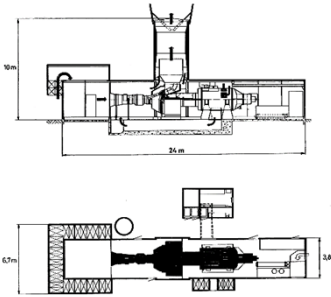
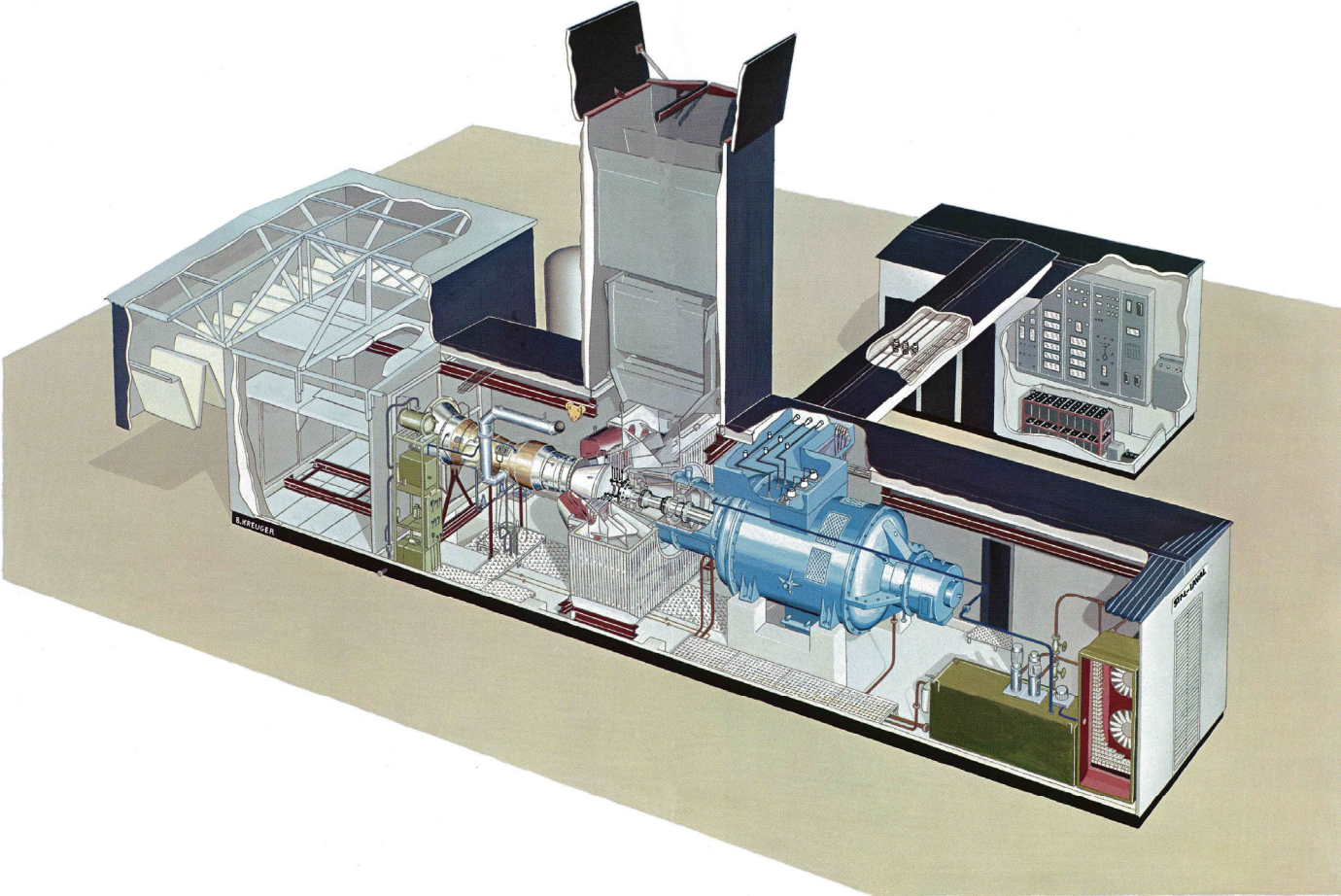


The gas turbine can handle higher air flow (~13 times), and thus producing far higher output.

- The gas turbine has a significantly lower weight per unit of power. Typically 1 tonne/MW (aero-derivatives), whilst the diesel engine is some 5 times higher.
- The gas turbine has a significantly lower volume per unit of power. It is typically 50 % of that of the diesel and increases with output

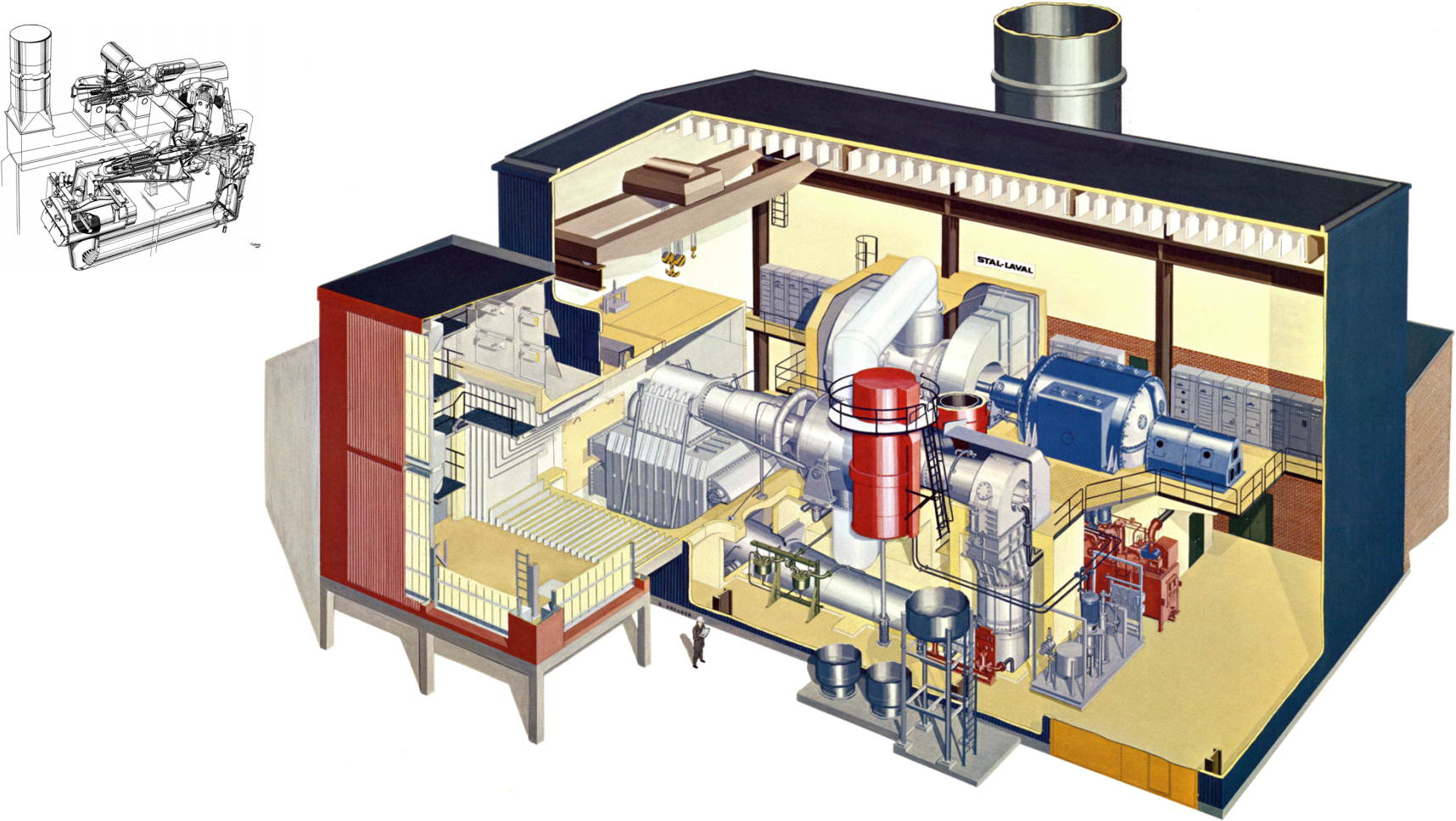


Power Pack – PP3

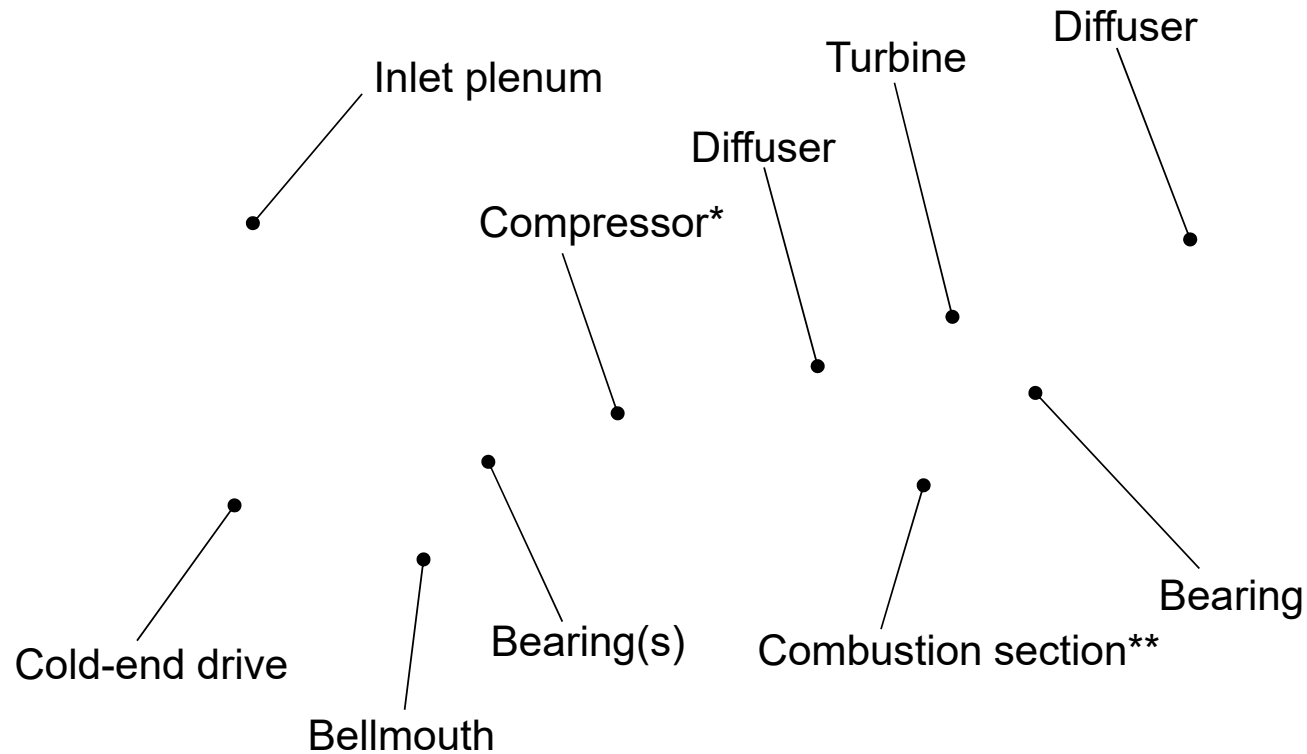


STAL-LAVAL GT-120

Late 50s 40...70 MW class, 21 units



Siemens SGT-800 – main parts



*15 stages PR \approx 22, 3 variable

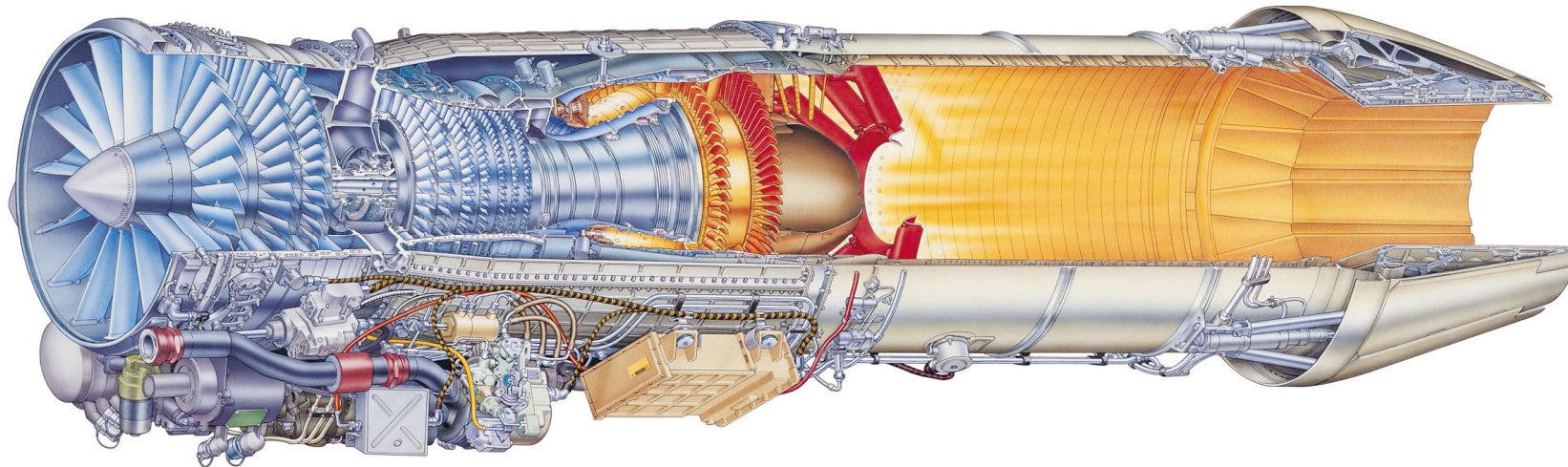
**Annular with 30 burners

Courtesy to Siemens



JAS Gripen engine - RM12

General Electric F404



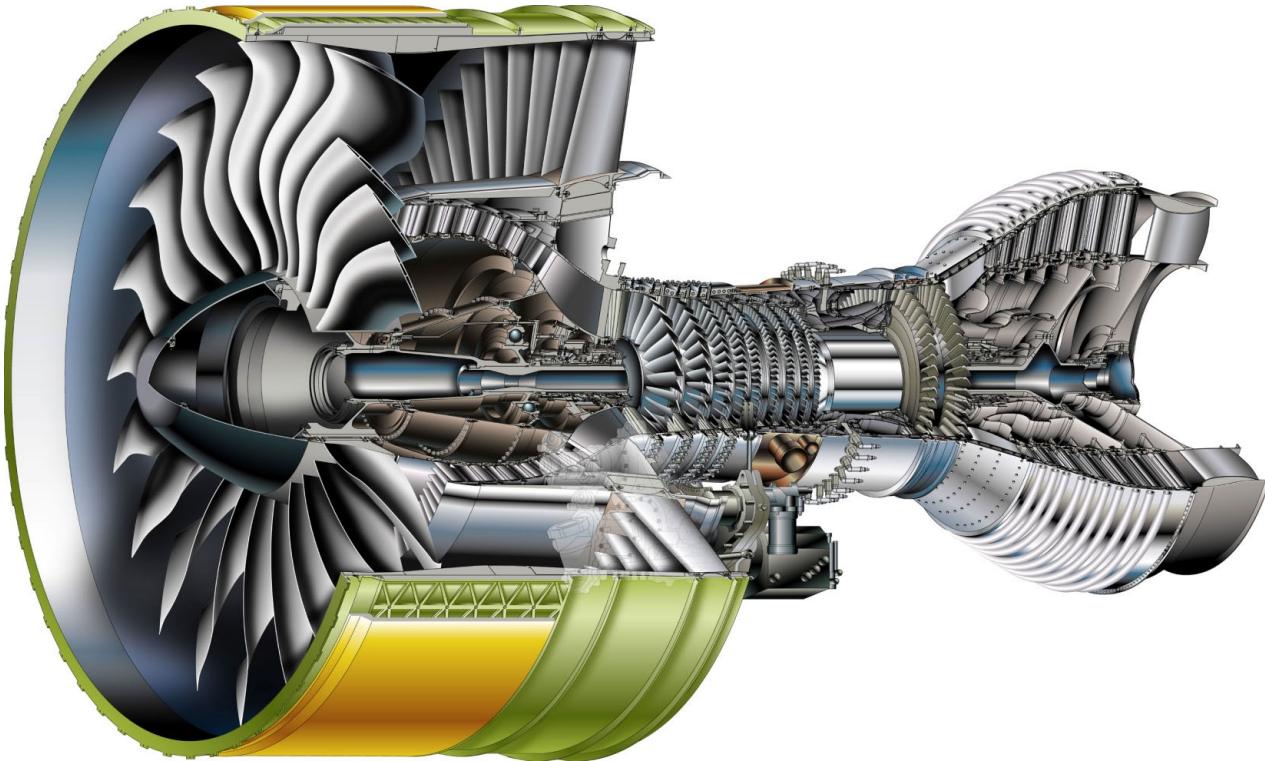
Thrust	54/80.5 kN
TSFC	23.9/50.1 g/kN·s)
PR	≈ 27.5:1
BPR	≈ 0.31:1
Flow	≈ 68 kg/s
Weight	≈ 1000 kg
Inlet diameter	≈ 0.79 m



Courtesy to Volvo Aero



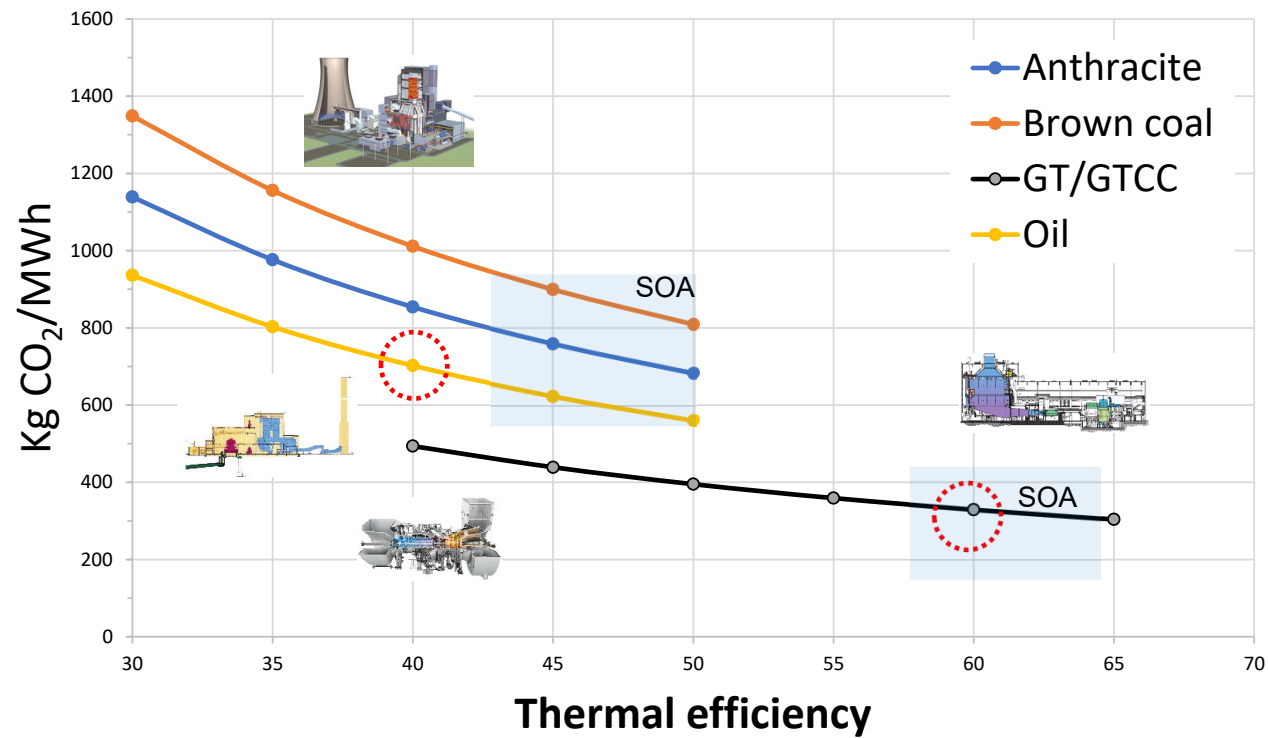
GE and Pratt & Whitney 7000-series (A380)



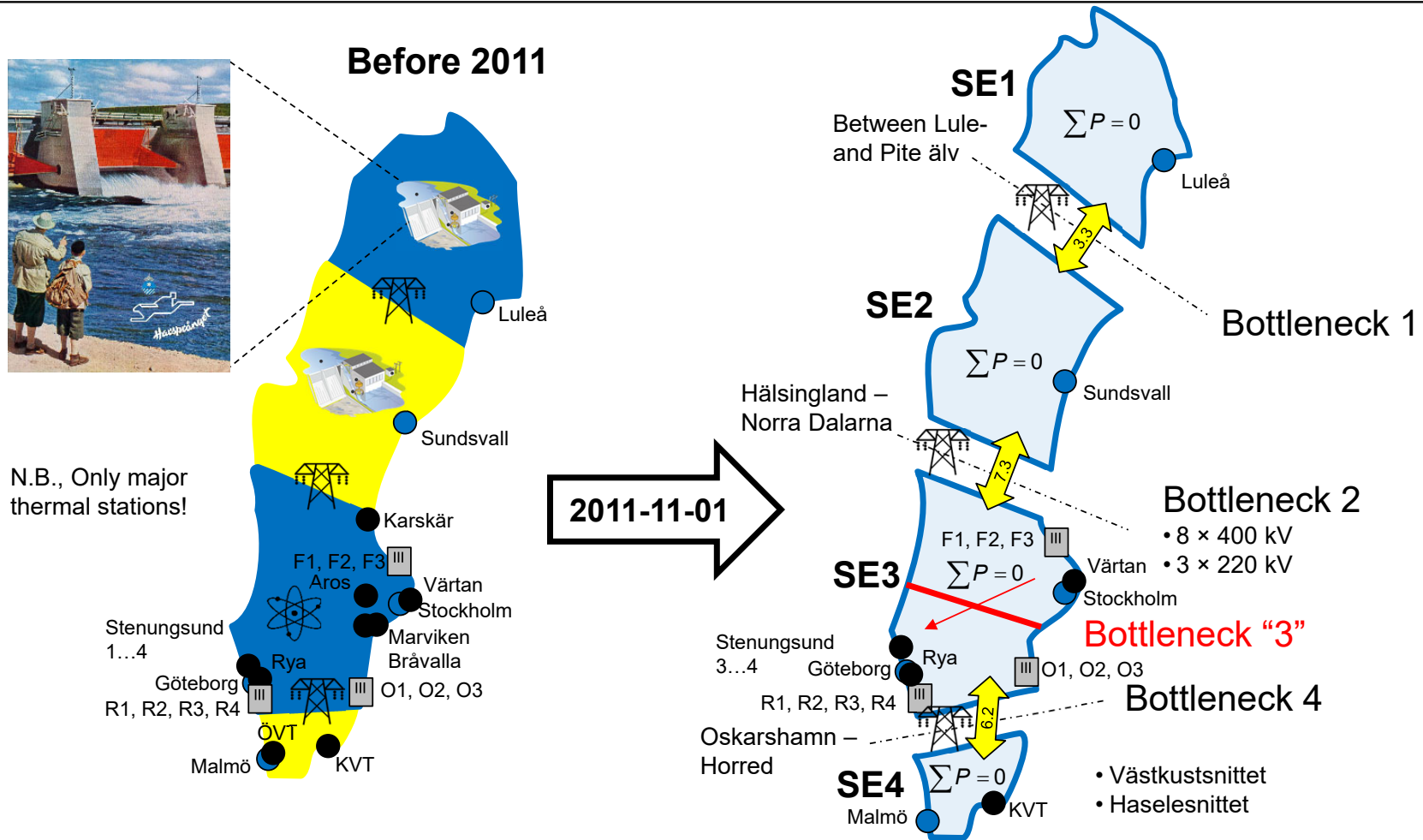
Emissions – CO₂



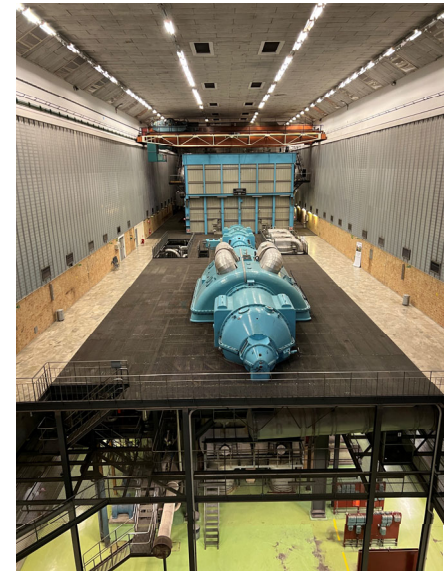
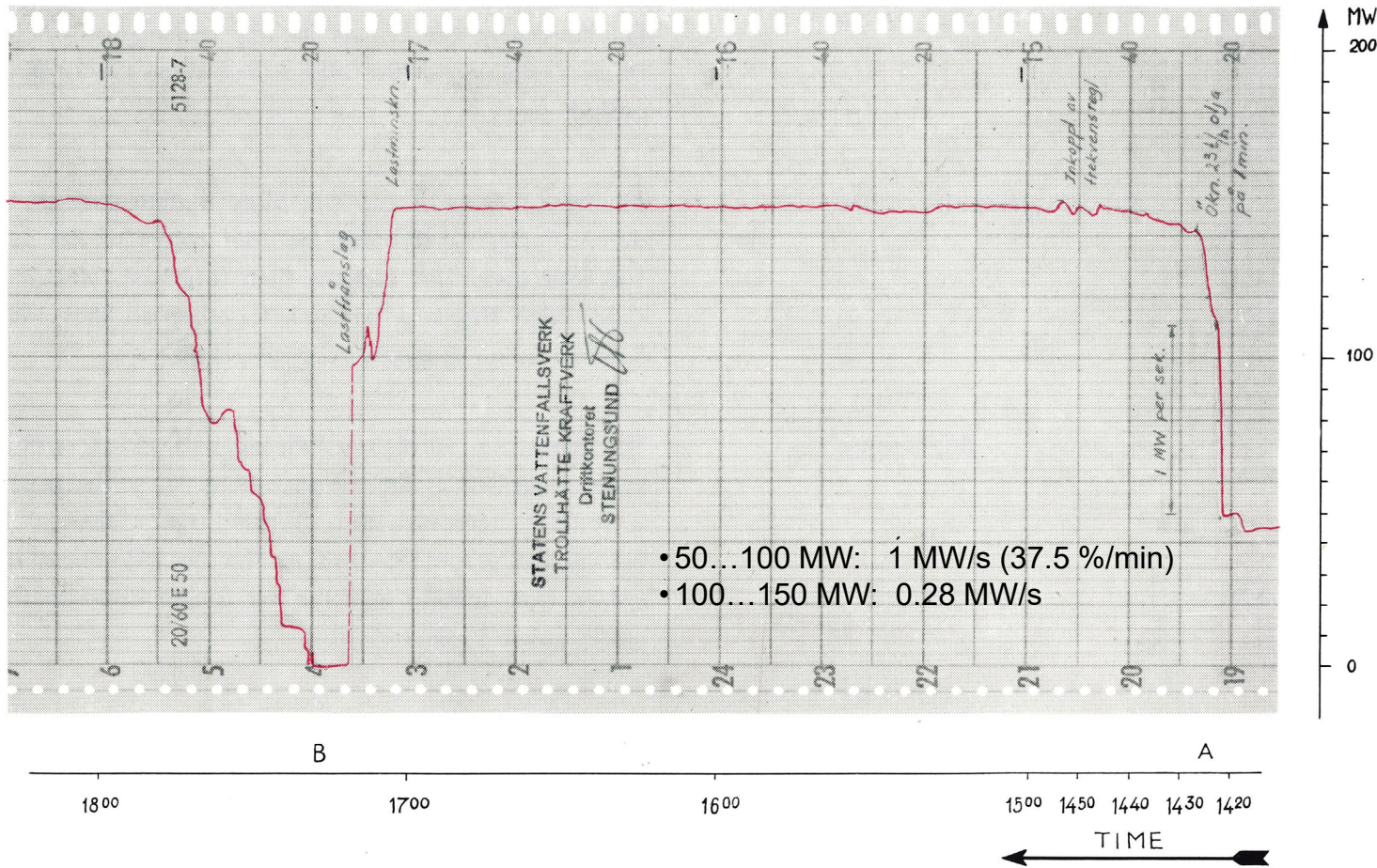
Carbon emission - CO₂/MWh



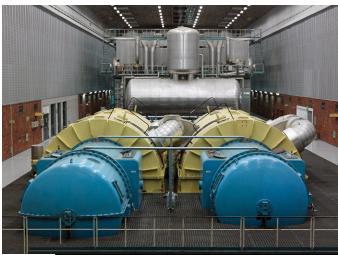
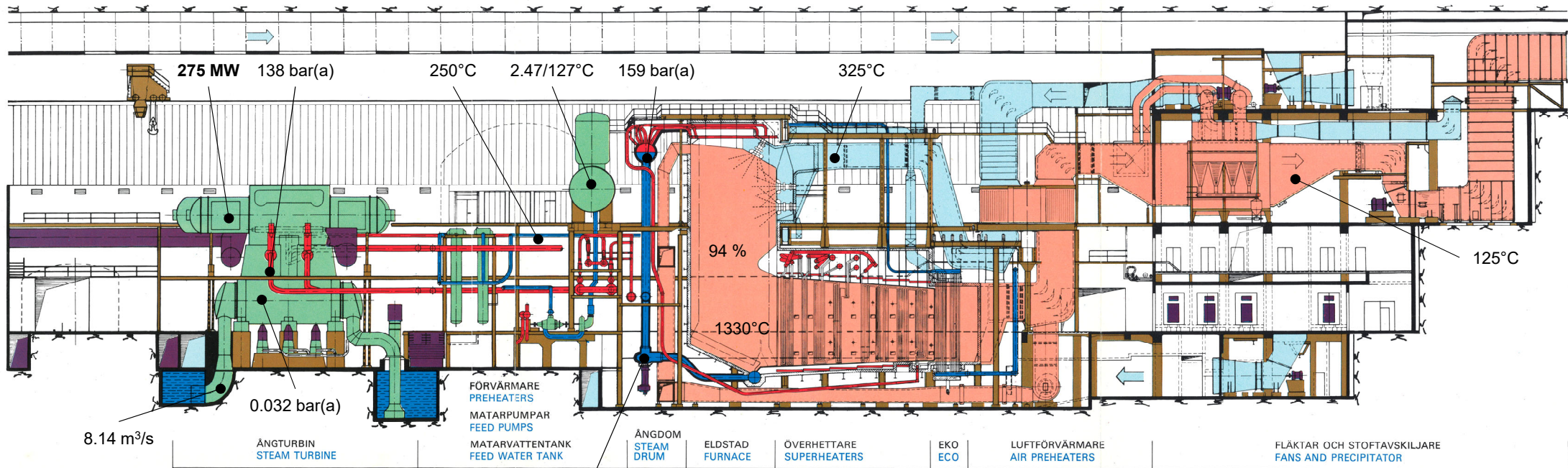
Production and transfer capacity – then and now...



Stenungsund unit 2 - 1960



Stenungsund QUAD-units 3 and 4 (1966-)

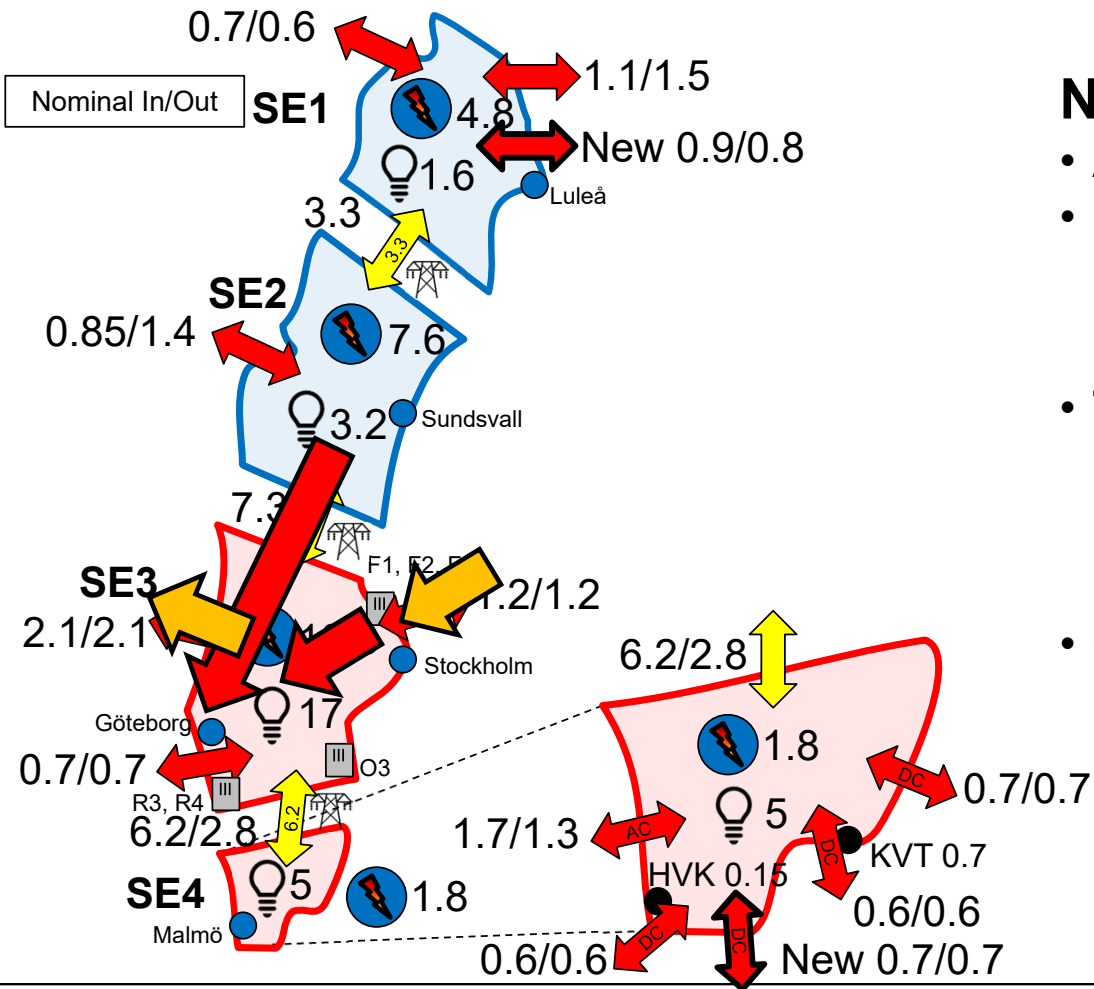


$\Delta p = 2.65 \text{ bar}$
 Flow = 3-400 kg/s
 CR \approx 5.3 –
 P = 450 kW

- 270 MW, 41.3 %
- Adm 145/25.2 bar(a)/530/540°C, 227 kg/s
- $p_{\text{cond}} = 0.032 \text{ bar(a)}$
- 4×5 m²
- $T_{\text{FW}} = 250^\circ\text{C}$
- Fuel = 16.1 kg/s



The current situation...



New flow patterns and scenarios!

- **Aurora (SE1)**
- **East-west flow (cf. R1 & R2)**
 - ✓ From Finland...
 - ✓ NO2 and DE
 - ✓ NO2 and UK
- **The west coast corridor**
 - ✓ Varying demand
 - ✓ High wind with northbound flow
 - ✓ Norwegian Hydro and new interconnectors
 - ✓ R1 & R2...
- **On hold Hansa PowerBridge - HPB (SE4)**

$$\frac{\sum \text{Export}_{@SE4}}{\text{Produktion}_{@SE4}} = \frac{3.2}{1.8} \approx 1.8$$

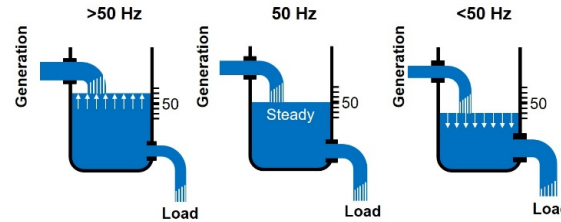




What is of utmost importance?

• Frequency stability

- ✓ 50 Hz (FCR-X, FRR, ...)
- ✓ Inertia...

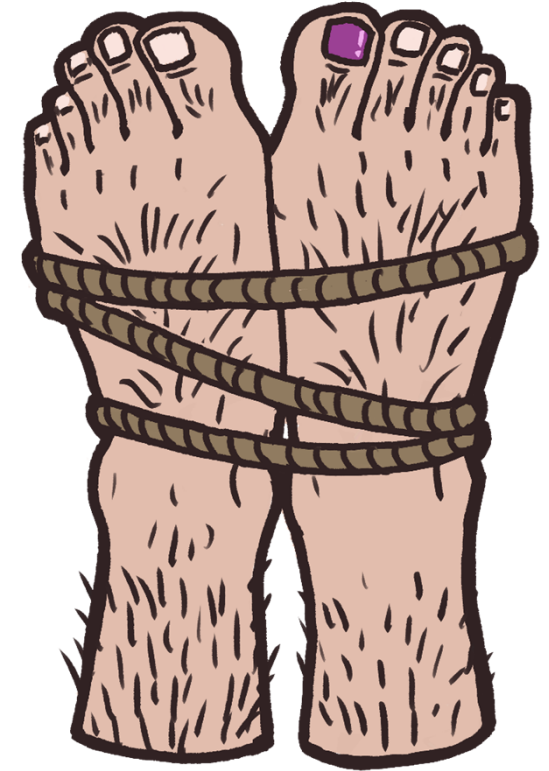


• Rotor angle stability

- ✓ The ability of interconnected machines of a power system to remain in synchronism during a disturbance
- ✓ The load angle and dynamic stability (cf. the equal area criteria)
- ✓ Inertia... $\Delta\phi \sim 1/H$
- ✓ Power system stabilizer – PSS during normal operation

• Voltage stability

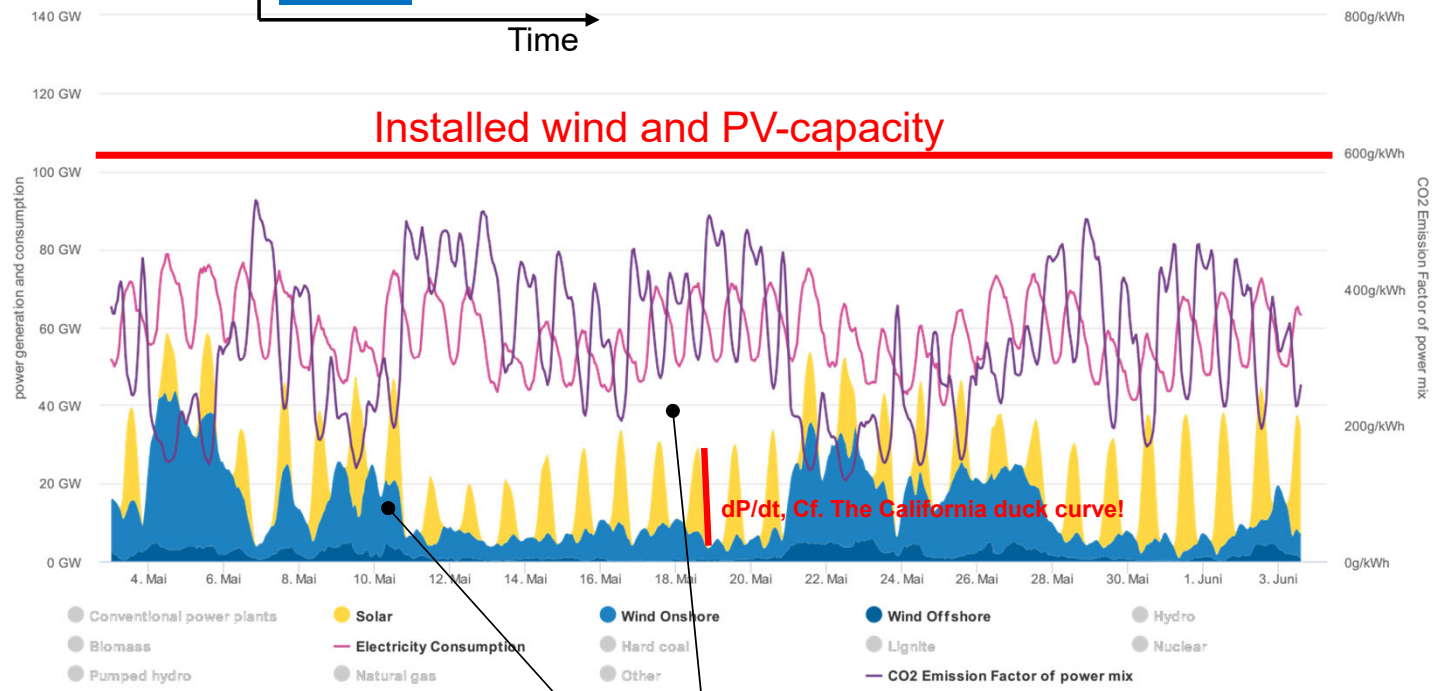
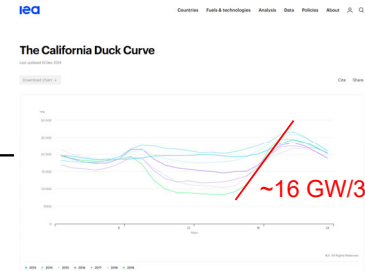
- ✓ The ability to maintain steady acceptable voltage at all buses in the system under normal operation – and after being subjected to a disturbance
- ✓ The main factor causing instability is the inability of the power system to meet the demand for reactive power. **The heart of the problem is usually the voltage drop that occurs when active- and reactive power through the inductive reactance associated with the transmission network**
- ✓ In recent years, voltage instability has been responsible for several major network collapses, such as New York (1970), Florida (1982), France (1978 and 1987), Belgium (1982), Sweden (1983 and 2003), and Japan (1987)



N.B., Study Kundur for an exhaustive treatment!



Germany May -21

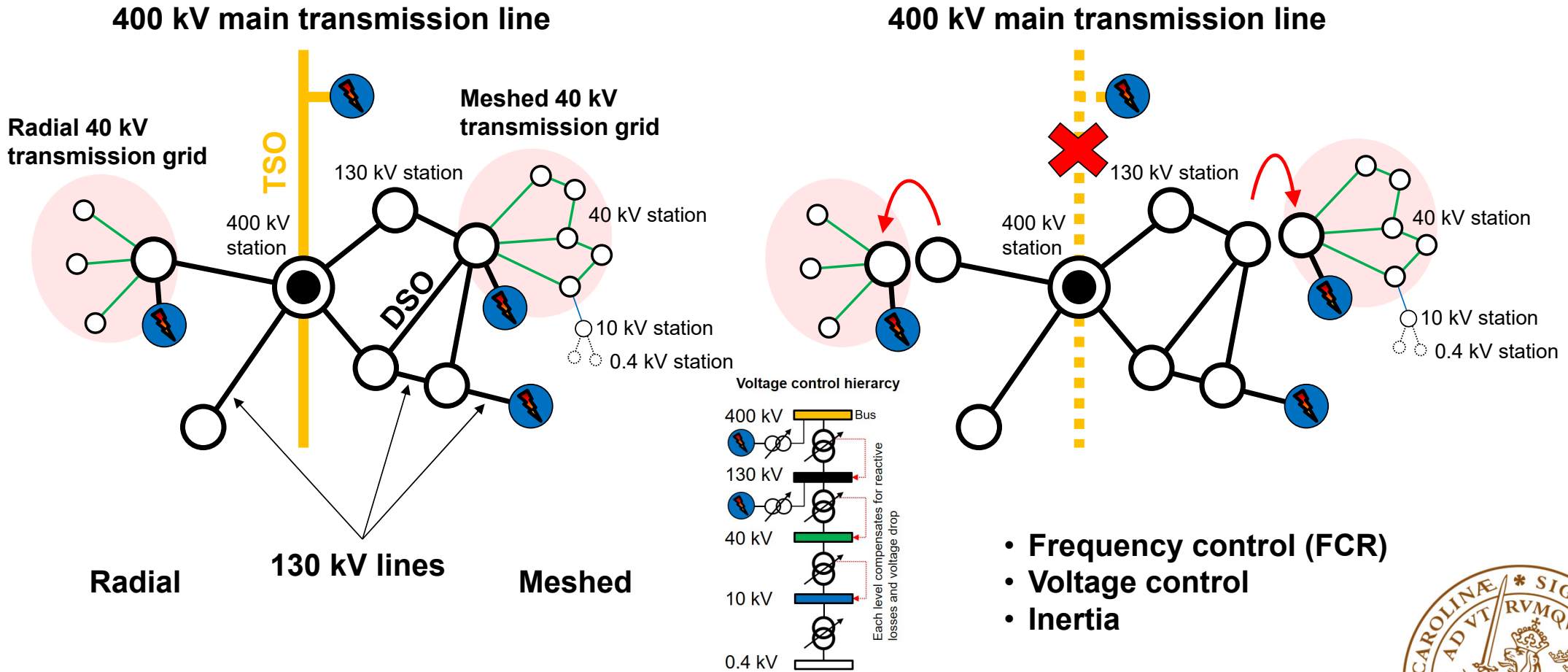


$$P\text{-ratio} = \frac{1}{LHV/HHV \prod_i (\eta_i)} \quad E_{Wind} = \int_0^{8760} P_{Wind} dt \approx 2.4 \dots 3.9 \int_0^{8760} P_{GT} dt$$

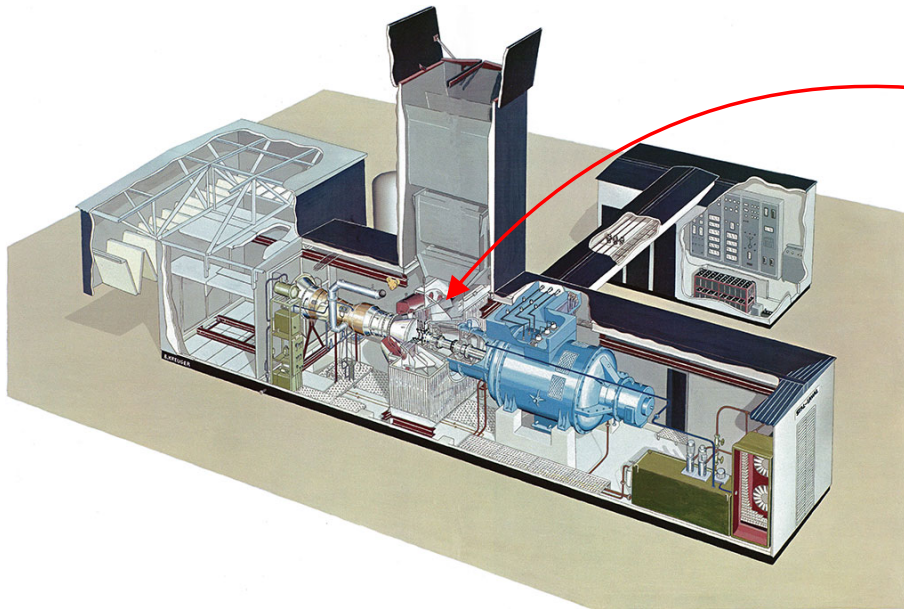
Agora Energiewende; Current to: 03.06.2021, 15:45



Black start and island mode – handling crisis and conflict



Power plants – PP3 and PP4



The current fleet:

- Modern single-shaft
- Old single-shaft
- Old multi-shaft
- Old aero-derivatives

Beyond 2025:

- Market
- All xFRR
- RfG-rules for FRT (5 min rule)?

Plant	Noff	Installed	Power	Firing	GG	A/C*	Vintage
STAL PP3	8	65...71	7...15	≤ 850°C	JT3C-6	B707/DC8	1950
STAL PP4	14	73...74	15...21	≤ 850°C	JT4A	B707/DC8	1955

JT3C 1950 → JT3D (T-fan) 1958
 JT4A 1955 → GG4/FT4

- JT3: B-52, KC-135, F-101, F-100, Sabre, F-8
- JT4: F-106, U-2, F-105



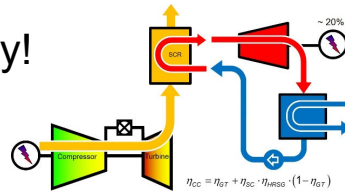
Gas turbines for SE3 and SE4?



• Renewable fuels

- Hydrogen
- e-Methanol
- Ammonia
- HVO
- Bio-gas

@64 % Efficiency!



• 5...10 minutes start

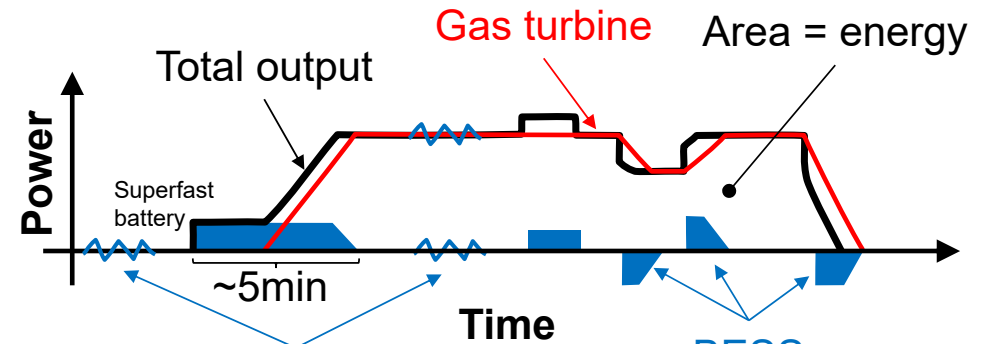
- GTCC within 30 min
- Future hot start capability 2 min for GT and 15 for GTCC

• A plethora of grid support

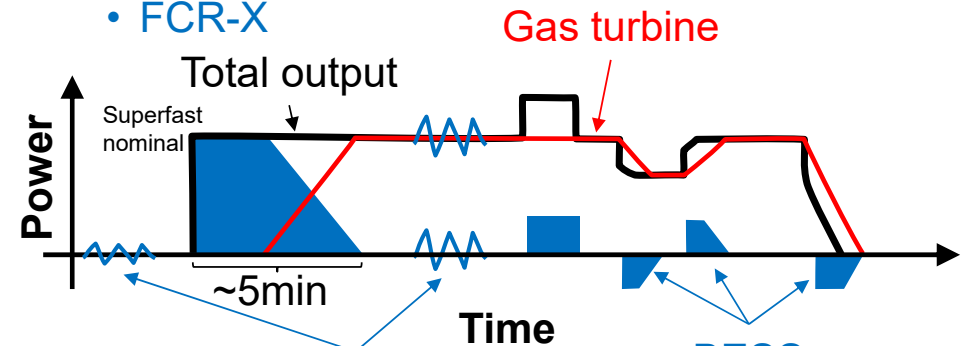
- FCR-N/FCR-D
- aFRR/mFRR (i.e., secondary and tertiary)
- Synchronous compensation (voltage/reactive power)
- Black start and island operation
- Inertia 1...3 and 5...~9 seconds (FRT)
- Short-circuit current

• Combine with battery and SSS-clutch

- FFR (~100...200 ms), FCR-D, xFRR, ... from the battery
- Voltage/reactive/short-circuit/inertia (24/7)
- No emissions!!! Hydrogen produces NOx!



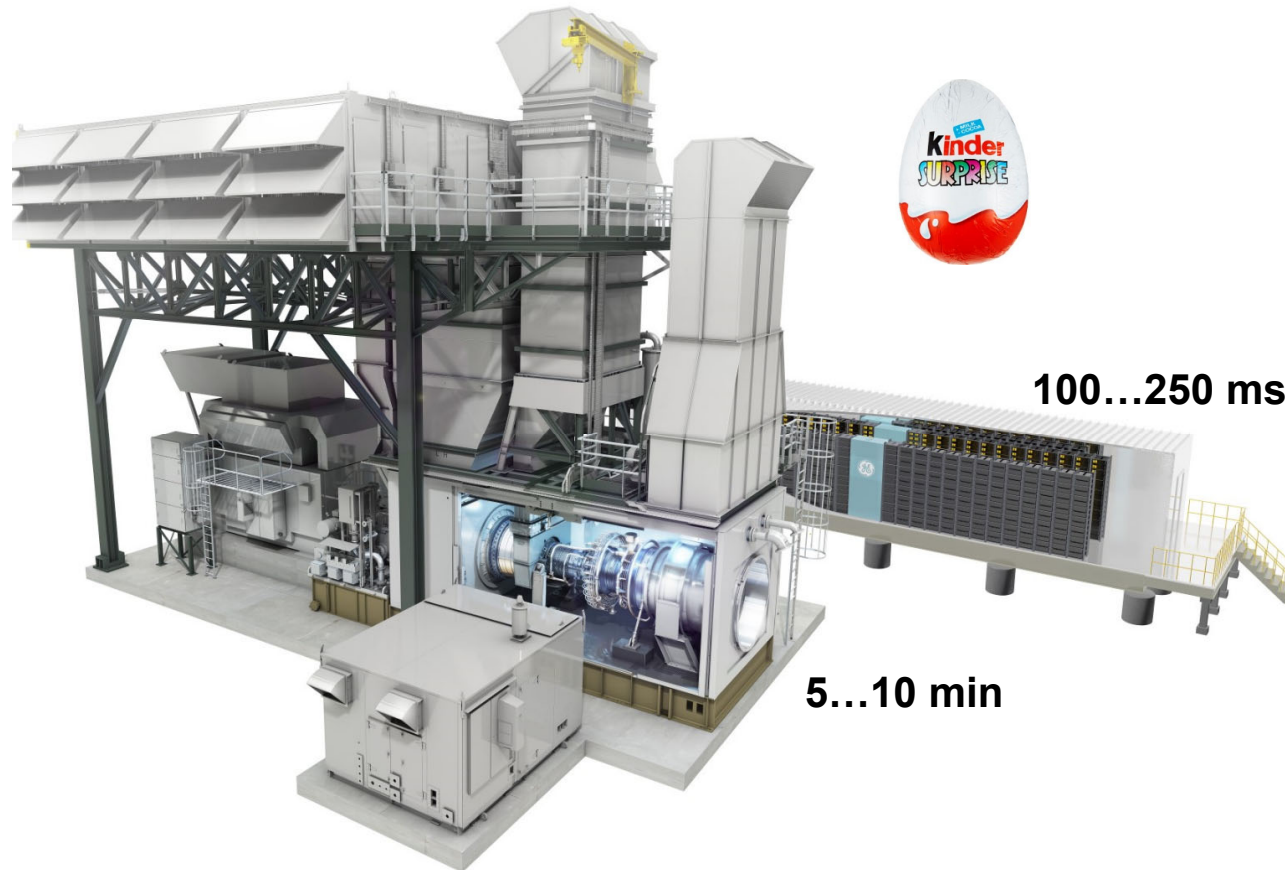
- RoCoF (~100 ms)
- FCR-X



- RoCoF (~100...200 ms)
- FCR-X



Gas turbine + BESS



10 MW Li Ion Battery

Attributes without Fuel Burn

- Instant response, always ready technology
- 50 MW of operating reserve
- Primary frequency response
- 5 to -8 MVAR voltage support
- 134 MW-secs inertia with synchronous condensing
- Black start technology
- Demand charge savings

Attributes with Fuel Burn

- 50 MW peaking energy for local contingency
- 25 MW of high speed frequency regulation
- 10MW peaking power
- Self-managed BESS state of charge

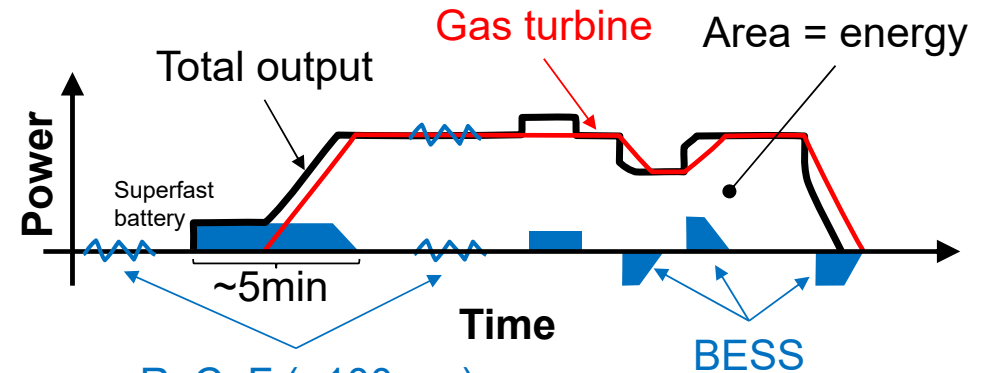
Courtesy to General Electric



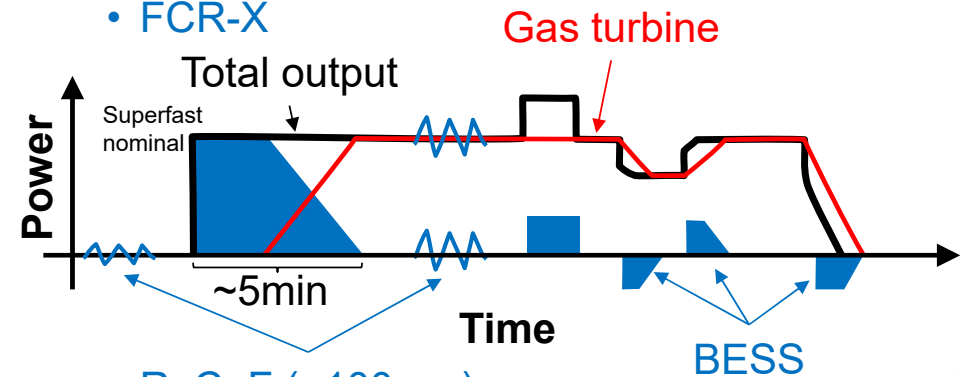
Gas turbine + BESS



- Combines FFR, FCR-X, and FRR
- Offers fast response (FFR) and persistent continuous operation (FRR)
- Fast hit 'n' runs without firing the gas turbine
- Size of battery?
- All aero derivatives and twin shafts have low H-values:
 - ✓ Can we use load banks or even the battery to prevent stepping out of phase?
 - ✓ Typically 40 kg·m² for a 1000 kg two-stage power turbine
- Lazard (-21) indicates 172...250 DC + 20...83 AC USD/kWh



- RoCoF (~100 ms)
- FCR-X



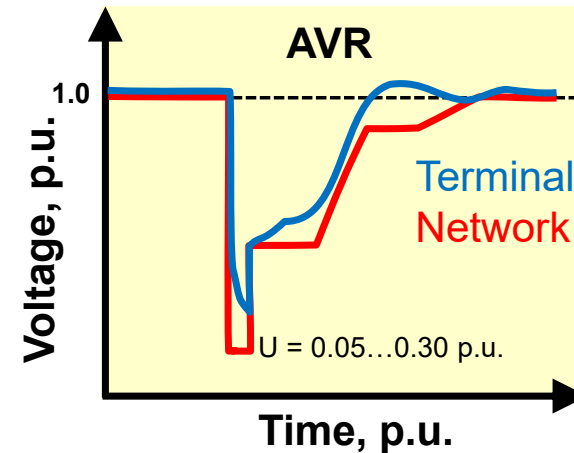
- RoCoF (~100 ms)
- FCR-X



FRT – Fault Ride Through capability



- Physical rotor angle at short circuit
 - $\Delta\varphi \sim 1/H$
- Load angle
 - Always below 90°
 - AVR response
- Fast breaking
 - Resistors (~ 500 ms)
 - Cf. Kundur p. 1106 (ed 1) or 881 (ed 2)



$$\left. \begin{aligned} \frac{df}{dt} &= \frac{\Delta P}{2 \cdot H \cdot P_{nom}} \cdot f_{nom} \\ \omega &= 2 \cdot \pi \cdot f \end{aligned} \right\} \therefore \frac{d\omega}{dt} = \frac{\pi \cdot \Delta P}{H \cdot P_{nom}} \cdot f_{nom}$$

$$\Delta\omega = \frac{\pi \cdot \Delta P}{H \cdot P_{nom}} \cdot f_{nom} \cdot t \Rightarrow \Delta\varphi_{rtr} = \frac{\pi \cdot \Delta P}{2 \cdot H \cdot P_{nom}} \cdot f_{nom} \cdot t^2 \xrightarrow[\Delta P = P_{nom}]{\text{Loss of power}} \Delta\varphi_{rtr} = \frac{90}{H} \cdot f_{nom} \cdot t^2 [^\circ]$$

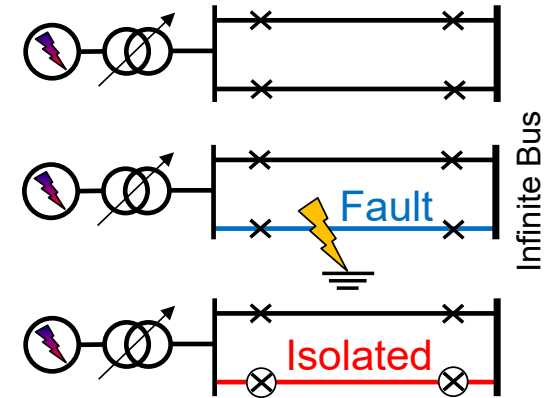
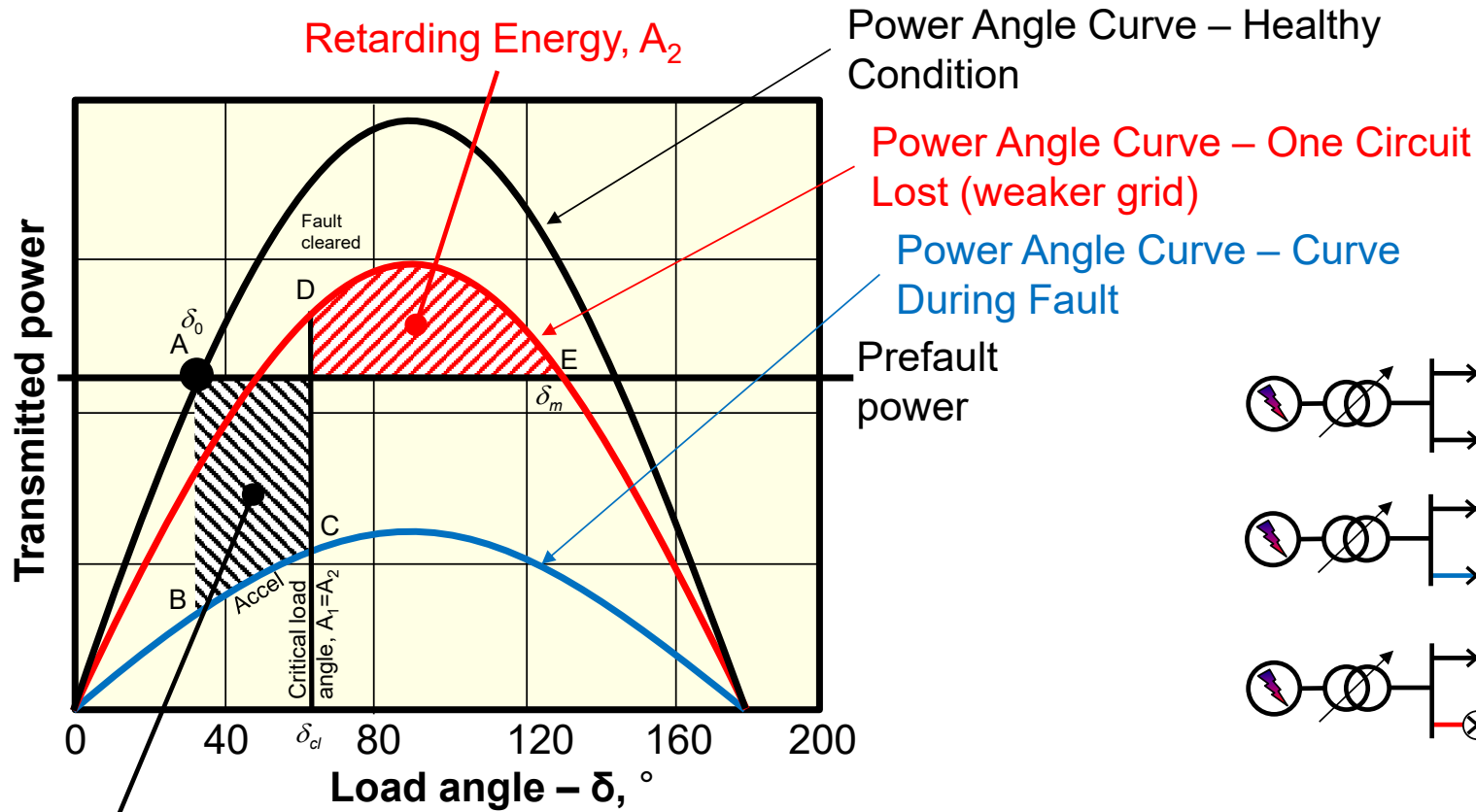
- Caveat! The load angle “ δ ” must also be taken into consideration ($\leq 90^\circ$). Cf. the literature on generators (equal area criteria)!
- Short-circuit torque variation – factor of 10! (miss-synchronization on the order of 20.)



The equal area criteria



Based on C.E.G.B

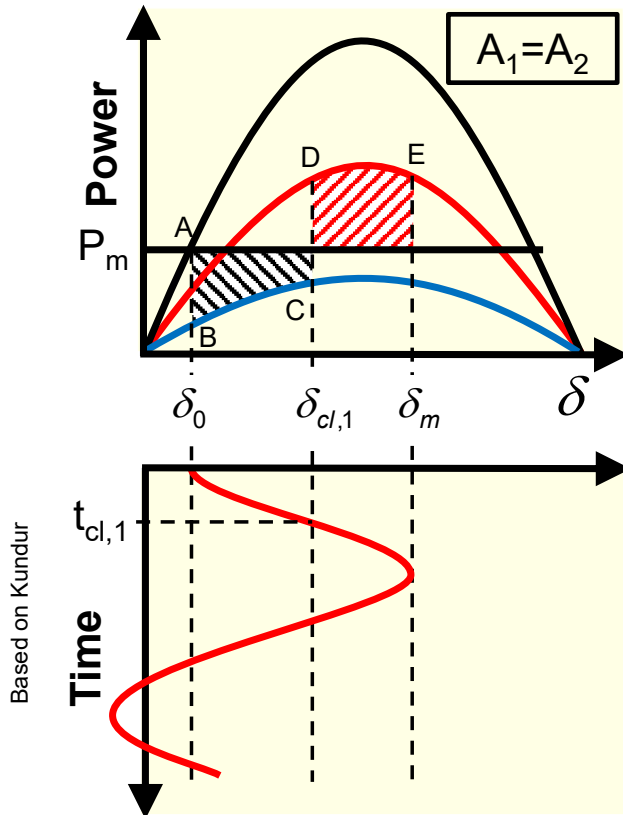


Accelerating Energy, A_1

The system is stable if the area A_1 is smaller than the area A_2 .



The equal area criteria cont'd



Stable case

1. When the fault occurs, the operating point suddenly changes from “A” to “B”. Owing to inertia, the load angle cannot change directly
2. The shaft power is larger than the electric power, and the rotor accelerates to “C”.
3. When the fault is cleared (by isolating line 2 from the system), the operating point suddenly shifts to “D”. **Now the electric power is higher than the shaft ditto, eventually causing deceleration.** The rotor speed is still higher than the nominal!
4. The rotor speed will continue to increase until the gained energy (i.e., A_1) is consumed, and we will reach point “E” at nominal speed – hence, A_2 equals A_1 !
5. Since the electric power is higher than the shaft power, the rotor decelerates below nominal (“E” to “D” and further down), and the load angle drops.
6. There will now be a new minimum load angle, which depends on the post-fault equal area criteria...
7. In the absence of **damping**¹, the system will continue to oscillate with constant amplitude!

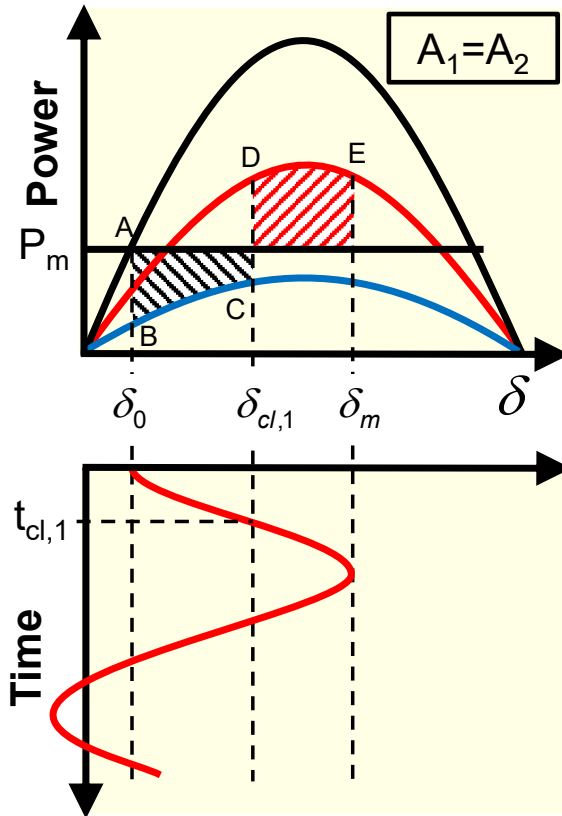
¹) Fast load reduction and exciter response (PSS)



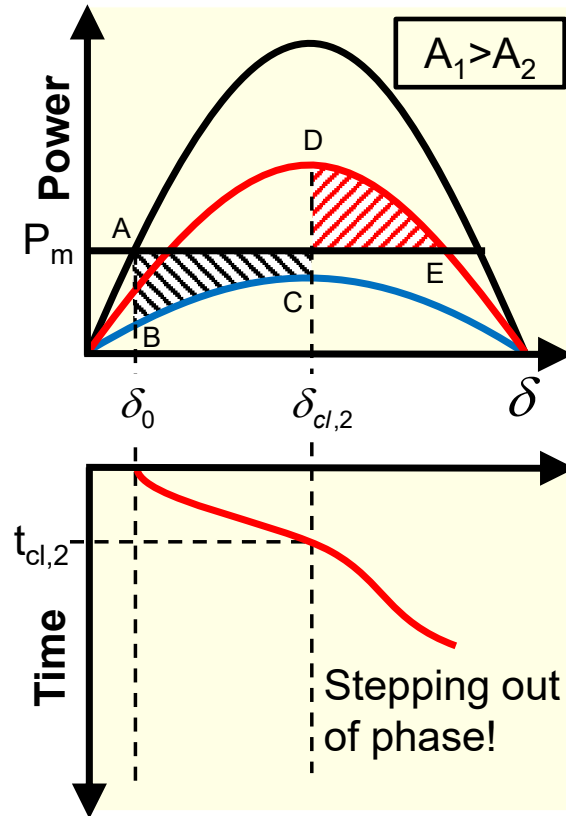
The equal area criteria cont'd



Based on Kundur



Stable case



Instability



Fault ride-through (FRT) capability – important factors

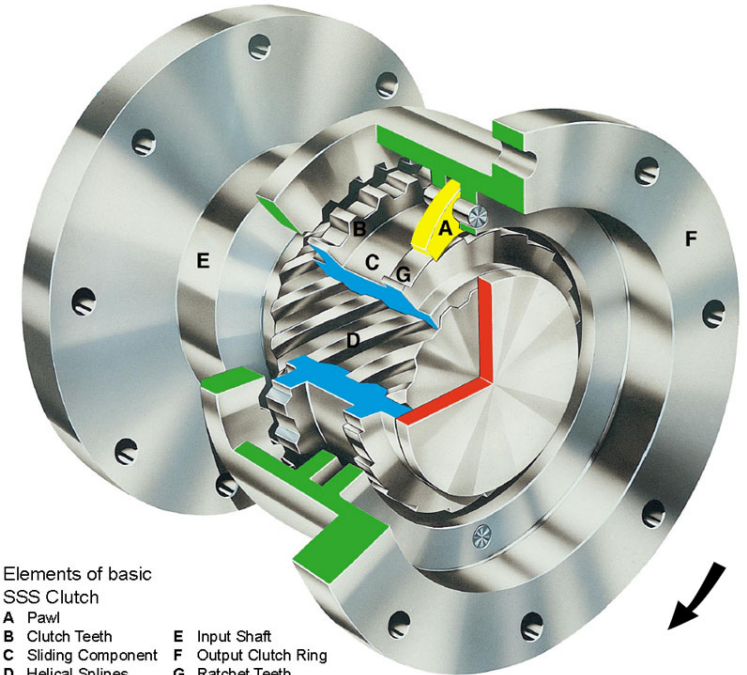
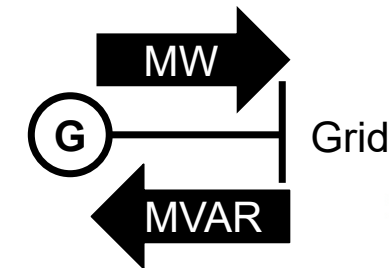
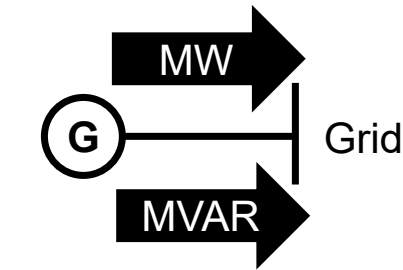
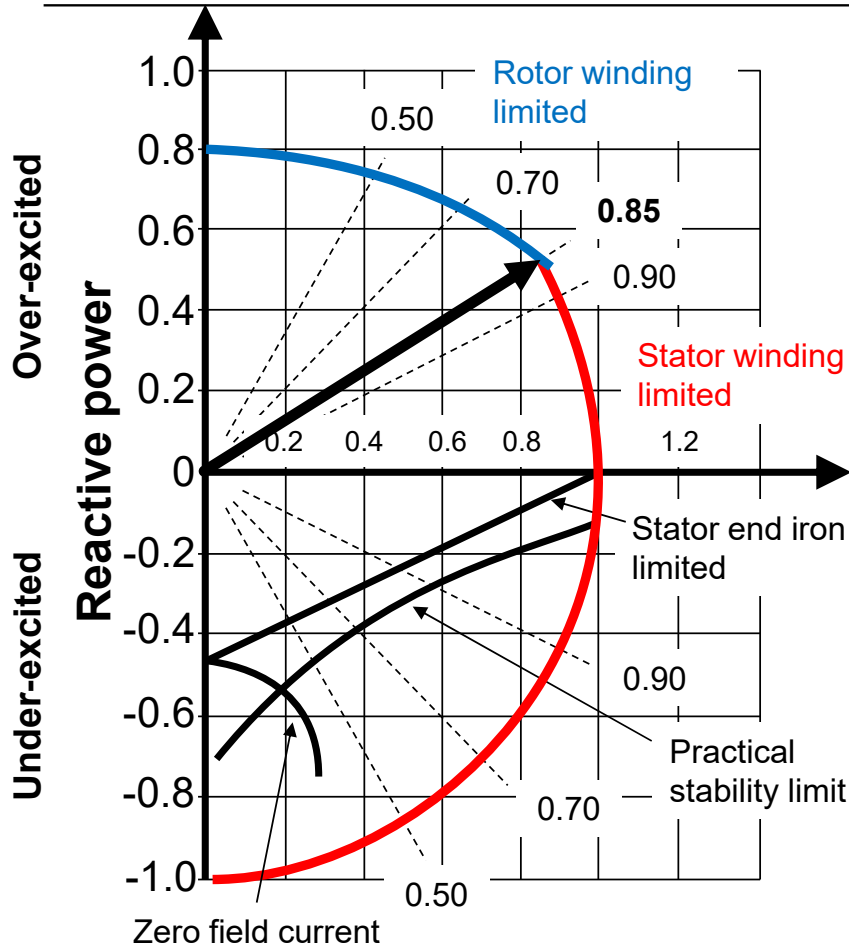


- The generator load before the fault
- The generator load during the fault – depends on the fault location and type.
 - For example, a meshed or radial grid
- The fault-clearing time
- The post-fault transmission system reactance
- The generator reactance, where lower increases peak power and reduces the initial load angle
- **The turbo-set inertia. The higher the inertia, the slower the rotor angle change rate. This reduces the gained kinetic energy during the fault – i.e., lower A_1 !**
- The generator's internal voltage, i.e., the exciter
- The infinite bus voltage magnitude

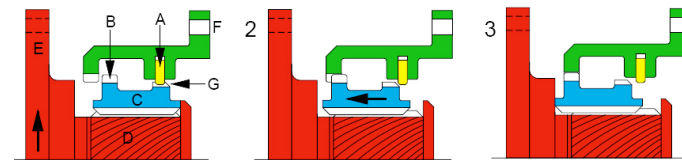
N.B., Study Kundur for an exhaustive treatment!



Alternator capability and SSS-clutch



- Elements of basic SSS Clutch
- A Pawl
 - B Clutch Teeth
 - C Sliding Component
 - D Helical Spines
 - E Input Shaft
 - F Output Clutch Ring
 - G Ratchet Teeth



SSS-clutches in Sweden – more than 43!



Year	Power – rating	Number of	Site	Engine
1969	50	4	Värtan	SL GT120
1969	20	2	Nondisclosed	SL PP3/PP4
1970	65	1	-"	V93
1970	65	1	-"	V93
1970	20	1	-"	SL PP3
1971 (1972)	70	3	-"	SL GT120
1971	30	6	-"	RR Avon
1971	30	2	-"	RR Avon
1971	30	2	-"	RR Avon
1971	20	4	-"	SL PP4
1972	20	2	-"	SL PP3
1973	20	4	-"	SL PP4
1974	80	2	-"	SL GT120
1974	30	4	-"	RR Avon
1975	35	4	-"	RR Avon

Synchronous condensation:

- Sweden has more than 43 SSS clutches installed
- Total installed SSS clutches in 2012 exceeded 550 units

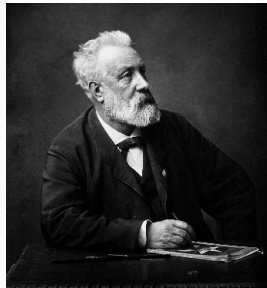


Hydrogen

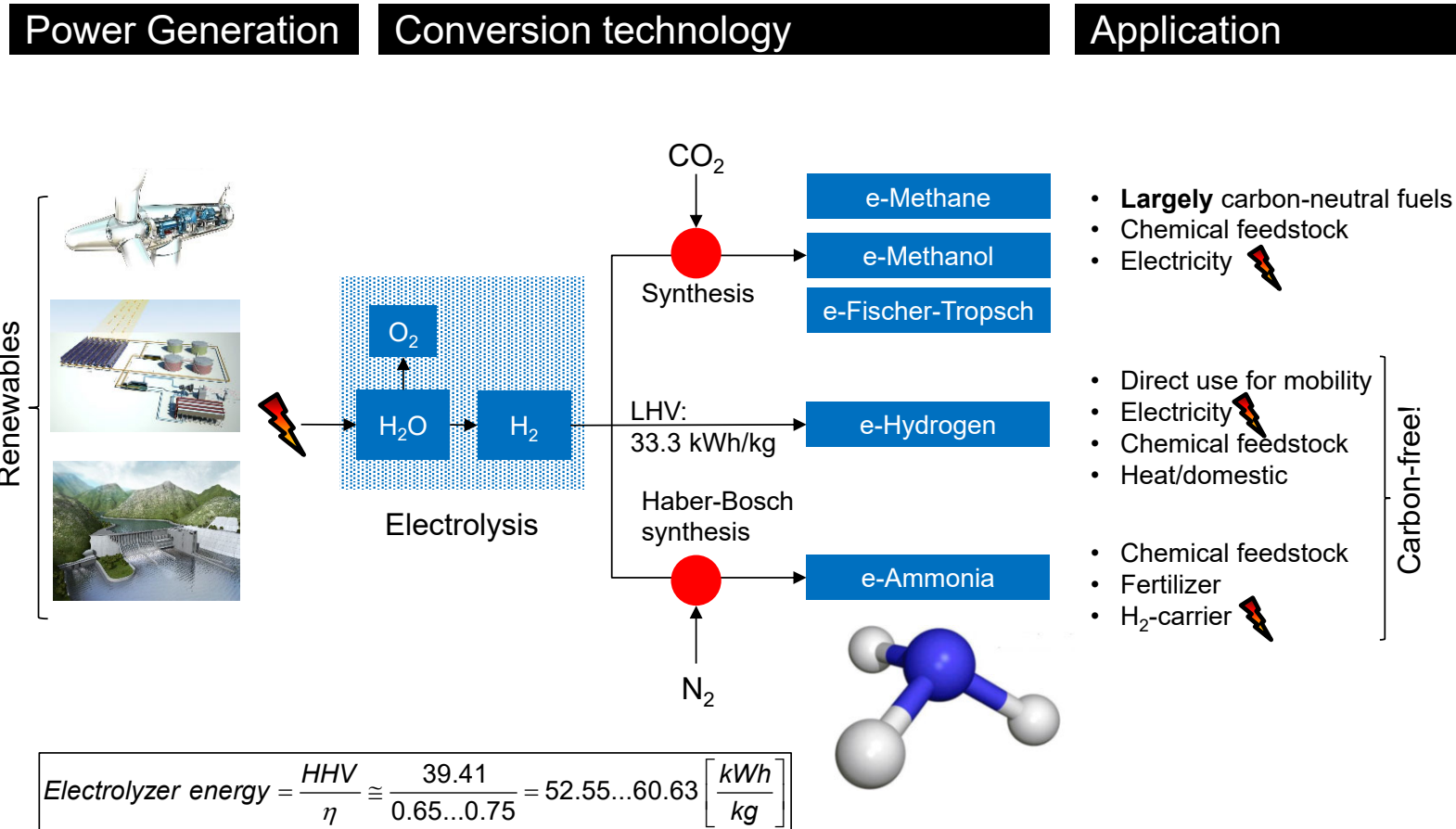


“...I believe that water will one day be employed as fuel, that hydrogen and oxygen which constitute it, used singly or together, will furnish an inexhaustible source of heat and light, of an intensity of which coal is not capable...”

Jules Verne – The Mysterious Island (L'Île mystérieuse), 1874



Power-to-Hydrogen and e-fuels



Ammonia – the flip side...



11:07 sön 18 apr. SYDSVENSKAN PREMIUM - FÖR DIG SOM PRENUMERERAR

KÄVLINGE 18 april 2021 10:00 Spara

25 år sedan ammoniakolyckan i Kävlinge: "Det var som en krigszon"

Under några dygn i april 1996 vändes allas blickar mot Kävlinge. Ett godståg spårade ur i en kurva mellan Kävlinge och Furulund och två vagnar lastade med 85 ton ammoniak välte. Det blev början på ett pådrag som varade i tre dygn och tvingade 9 000 människor att lämna sina hem.

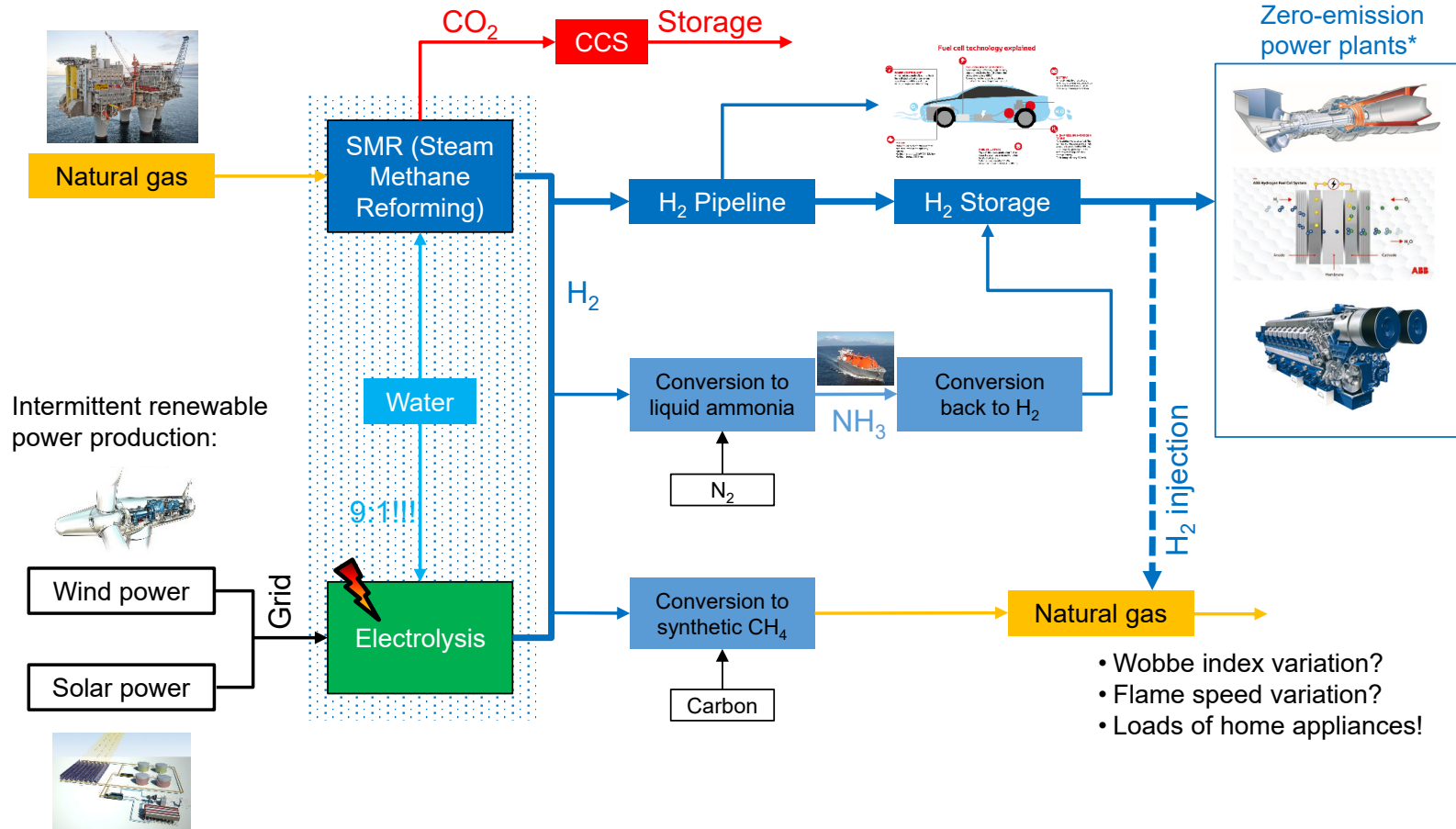
Emelie Malmros + Följ Maria Schlin + Följ



Vid olyckan spårade nio vagnar ur. De två välta tankvagnarna innehöll 45 respektive 40 ton ammoniak, vilket krävde ett stort säkerhetspådrag. Bild: Peter Kroon



Hydrogen – possibilities for power



*64% (+) efficiency for GTCC

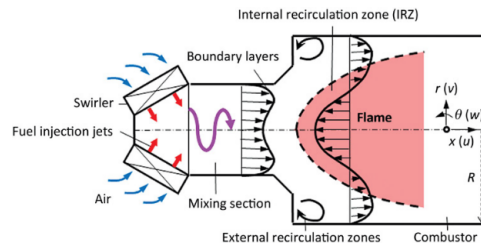


Hydrogen – key fuel characteristics



H ₂ -blend in pipeline natural gas						
H ₂ -blend (%-vol)	0	5	10	20	30	100
Laminar flame speed ¹ [cm/s]	124	127	130	139	150	749
Autoignition delay time ² [ms]	124	112	107	104	103	76
Rel Wobbe index	1	0.987	0.974	0.947	0.919	0.855
Flame temperature ³ [°C]	2,319	2,321	2,324	2,329	2,337	2,488
Flammability (%-vol LEL)	4.88	4.83	4.79	4.71	4.63	4
H ₂ -blend (%-vol)	0	5	10	20	30	100

Benim & Syed: Flashback Mechanisms in Lean Premixed Gas Turbine Combustion



- 1) Calculated for equivalence ratio 1.0 @ 316°C/1 atm
- 2) Calculated for equivalence ratio 0.4 @ 649°C/1 atm
- 3) Adiabatic stoichiometric for a typical gas turbine

$$\frac{2 \left[\frac{\text{USD}}{\text{kg}} \right]}{120 \left[\frac{\text{MJ}}{\text{kg}} \right]} \cdot 3600 \left[\frac{\text{s}}{\text{h}} \right] = 60 \left[\frac{\text{USD}}{\text{MWh}} \right] = 30 \cdot f \left[\frac{\text{USD}}{\text{kg}} \right]$$

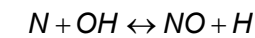
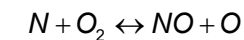
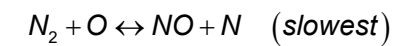
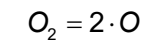
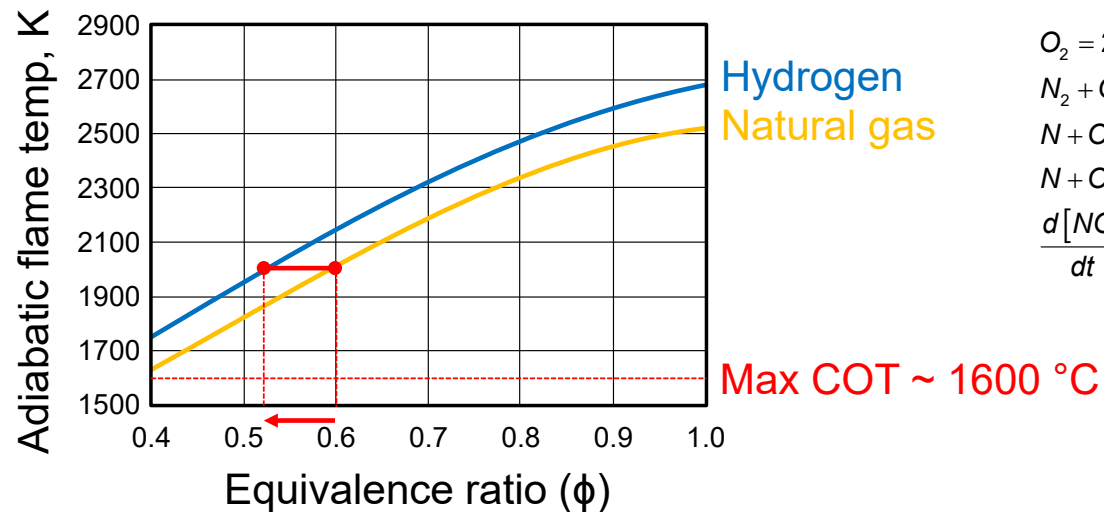
$$\text{Electrolyzer energy} = \frac{HHV}{\eta} \cong \frac{39.41}{0.65 \dots 0.75} = 52.55 \dots 60.63 \left[\frac{\text{kWh}}{\text{kg}} \right]$$

- Hydrogen storage:
- 39.2 kg/m³@700 bar/25°C
 - 67.7/2.5 kg/m³@2bar/-250.2°C





Hydrogen – flame temperature



$$\frac{d[NO]}{dt} = C_1 \cdot T^{-\frac{1}{2}} \cdot e^{-\frac{69090}{T}} \cdot [N_2] \cdot [O_2]^{\frac{1}{2}}$$

How do we fix the NOx-issue?

- Higher adiabatic flame temperature with hydrogen...
- Increasing NOx with increasing temperature – the rate roughly doubles (!) in magnitude for each 20°C a.k.a the “misery factor
- Two principal things to do – more lean or/and reduced residence time



Hydrogen, Ammonia and Methane



		Methane	Hydrogen	Ammonia
Molecule		CH ₄	H ₂	NH ₃
Molecular weight	g/mol	16	2	17
Boiling temperature	°C	-161.5	-252.9	-33.3
Lower/upper flammability limits	%	4.4/17	4/75	15/28
Flame speed	cm/s	~30...40	~200...300	~6...7
Burner exit velocity	m/s	60...75	?	?
Adiabatic flame temperature	°C	1,963	2,204	1,799
Lower heating value	MJ/Nm ³	35.8	10.8	14.1
Lower heating value	MJ/kg	50.0	120.0	18.6
Lower heating value	kWh/kg	13.9	33.3	5.2
NO _x impact (relative to CH ₄)	-	1	~2×	~150×

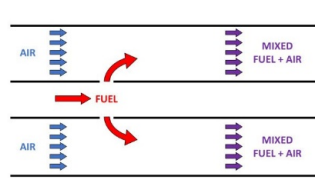
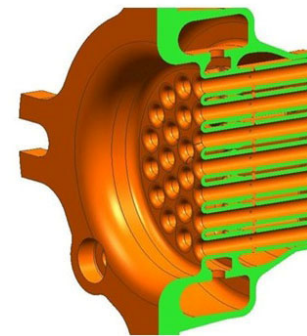
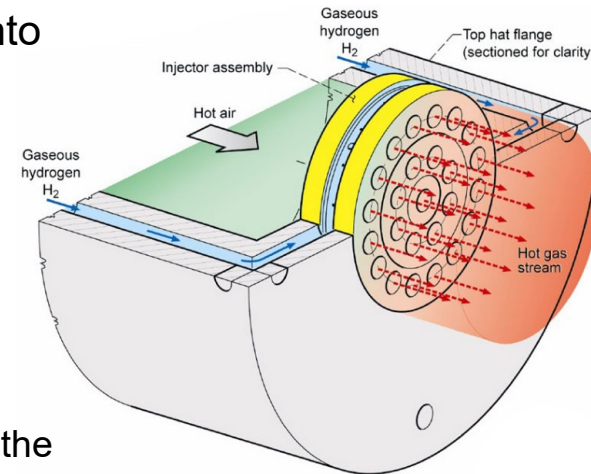
Critical swirl number is 0.5...0.6



NASA hydrogen combustor – LDI



- Normal “swirl-based” DLE-systems may run into severe issues:
 - ✓ Flashback
 - ✓ Flame holding
- **Lean Direct Injection – LDI**
 - ✓ Rapid mixing
 - ✓ Loads of small-scale mixers
 - ✓ Bulk velocity leaving the mixer is higher than the flame speed
 - ✓ Hole diameter less than the quench distance of the flame – little risk for flame holding within the tubes
- General Electric DLN2.6e

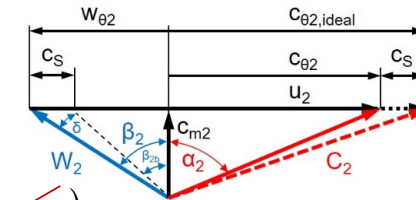


Hydrogen compression – a stress thing!



	NG	H ₂
η_p [-]	0.87	0.87
$\gamma = c_p/c_v$ [-]	1.468	1.412
M [kg/kmol]	17.185	2.016
T_0 [K]	288.15	
a_0 [m/s]	452	1296
u_2 [m/s]	700 (!!!) $\sigma \sim u^2$	
$M_{u,2}$ [-]	1.55	0.54
$\beta_{2,b}$ [°]	-45 (0)	0
Z [-]	18	18
α_2 [°]	71*	
$\Delta h_0/u_2^2$ [-]	0.70 (0.87)	0.87
PR [-]	4.82 (6.38)	1.34
$N_{off,rel}$ [-]	1	5.3 (6.3)

* $\lambda \approx 2.9$



Basic equations:

$$\Delta h_0 = \omega(r_2 \cdot c_{\theta,2} - r_1 \cdot c_{\theta,1})$$

$$c_{\theta,2} = u_2 + c_m \cdot \tan \beta_{2,b} - c_{slip}$$

$$\frac{\Delta h_0}{u_2^2} = \frac{\Delta c_\theta}{u} = 1 - \underbrace{\frac{c_{slip}}{u_2}}_{\sigma} + \frac{c_{m,2}}{u_2} \tan \beta_{2,b} = \frac{\sigma}{1 - \frac{\tan \beta_{2,b}}{\lambda}}$$

Wiesner slip factor:

$$\sigma = 1 - \frac{\sqrt{\cos \beta_{2,b}}}{Z^{0.7}}$$

$$PR = \left[1 + (\gamma - 1) \frac{\Delta h_0}{u_2^2} M_{u2}^2 \right]^{\eta_p \frac{\gamma}{\gamma - 1}}$$

N.B., each stage must be inter-cooled!!!

Blade Mach number:

$$M_{u2} = \frac{u_2}{\sqrt{\gamma RT_{01}}}$$



Cost of Electricity – COE



COE = CAPEX + OPEX

$$COE = \underbrace{\frac{\beta \cdot CAPEX}{P \cdot H}}_{\text{Capital}} + \underbrace{\frac{f}{\eta}}_{\text{Fuel}} + \underbrace{\left\{ \frac{OM_{fix}}{P \cdot H} + \mu \cdot OM_{var} \right\}}_{\text{Maintenance}} \left[\frac{\text{money unit}}{kWh} \right]$$

$$COE = \frac{\beta \cdot CAPEX}{P_{eff} \cdot H_{eff}} + \frac{f}{\eta_{eff}} + \left\{ \frac{OM_{fix}}{P \cdot H} + \mu \cdot OM_{var} \right\} + \underbrace{\sum_{i=1}^n (c_i \cdot m_{p,i})}_{\text{Emissions}} + \underbrace{\frac{S_c \cdot \Delta P + S_e \cdot \Delta E}{P_{eff} \cdot H_{eff}}}_{\text{Replacement capacity}}$$

$$H_2 @ 2 \left[\frac{USD}{kg} \right] : \frac{60 \cdot 5}{2} = 150 \left[\frac{USD}{MWh} \right]$$

$$H_2 @ 4 \left[\frac{USD}{kg} \right] : \frac{120 \cdot 5}{2} = 300 \left[\frac{USD}{MWh} \right]$$

Where:

$$\beta(i, N) = \left[\frac{i(1+i)^N}{(1+i)^N - 1} \right] \quad \text{10 percent interest rate (i) and 25 years (N) gives } \beta = 0.11$$

$$f = \underbrace{f_0 \cdot k}_{USD/MMBtu} \cdot \underbrace{0.947817 \cdot 10^{-3}}_{[MMBtu/MJ]} \cdot \underbrace{3.6}_{[MJ/kWh]} = \frac{f_0 \cdot k}{293.071} \quad [USD/kWh]$$

$$\frac{CAPEX}{P} \approx (1.6 \dots 1.8 \dots 2.0) \cdot \begin{cases} S/C : 4098 \cdot P^{-0.0843} - 1216 & [USD/kW] \\ GTCC : 337 + 6.58 \cdot 10^4 \cdot P^{-0.38} \end{cases}$$

$$OM_{var} \approx (3.0 \dots 3.5 \dots 5.0) \cdot 10^{-3} \quad [USD/kWh]$$

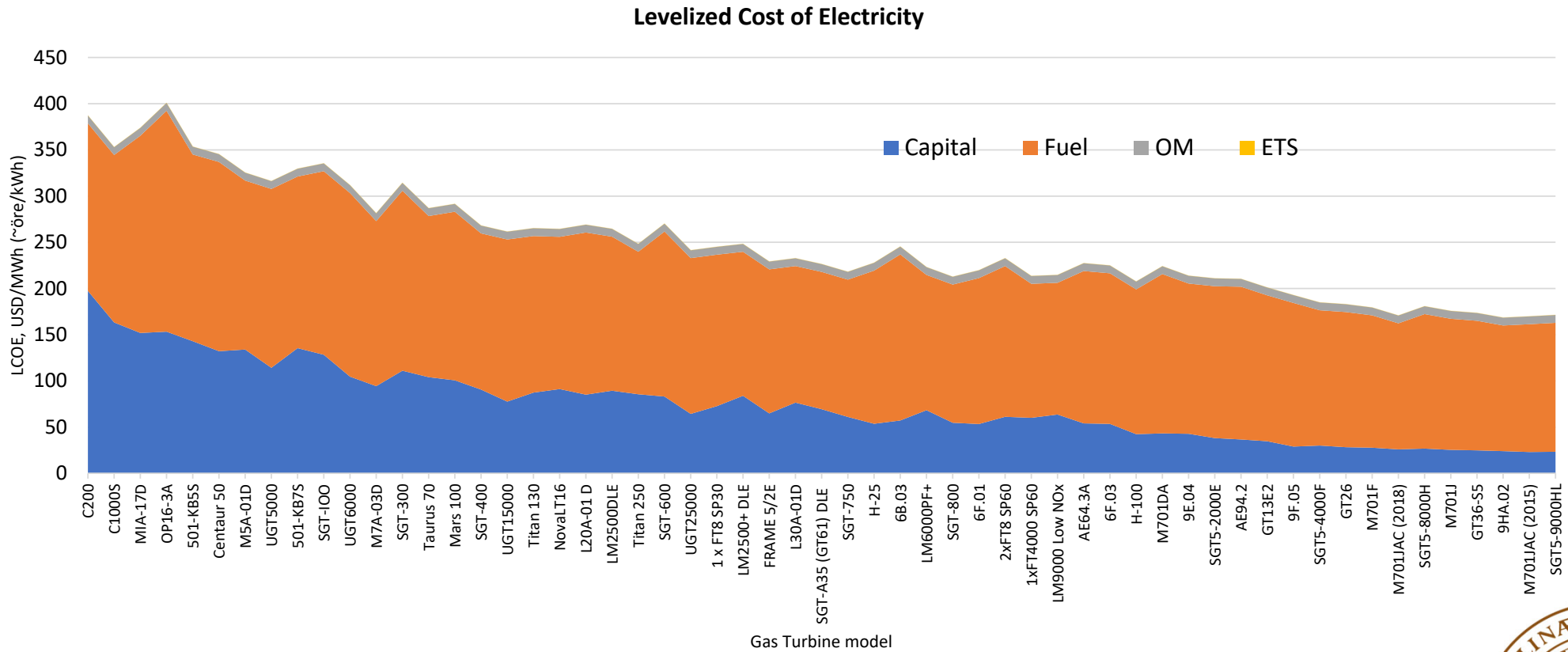
$$OM = \underbrace{10 \dots 16}_{\text{per annum}} \left[\frac{USD}{kW_{installed}} \right] + (3.5 \dots 5.0) \cdot 10^{-3} \quad [USD/kWh]$$

CAPEX	Capital Expenditure
β	Annuity factor
P	Power
H	Annual operating hours
f	Fuel cost [USD/kWh]
i	Interest rate
N	Number of years
OM_{fix}	Fixed OM-spending [USD]
OM_{var}	Variable OM-spending [USD/kWh]

N.B. All OM costs are engine dependent! One may (typically) expect a service cost equivalent to a new engine during 80,000 operating hours. The total service market will exceed 41 BUSD 2025!



Hydrogen @ 60 USD/MWh – a feasible solution?



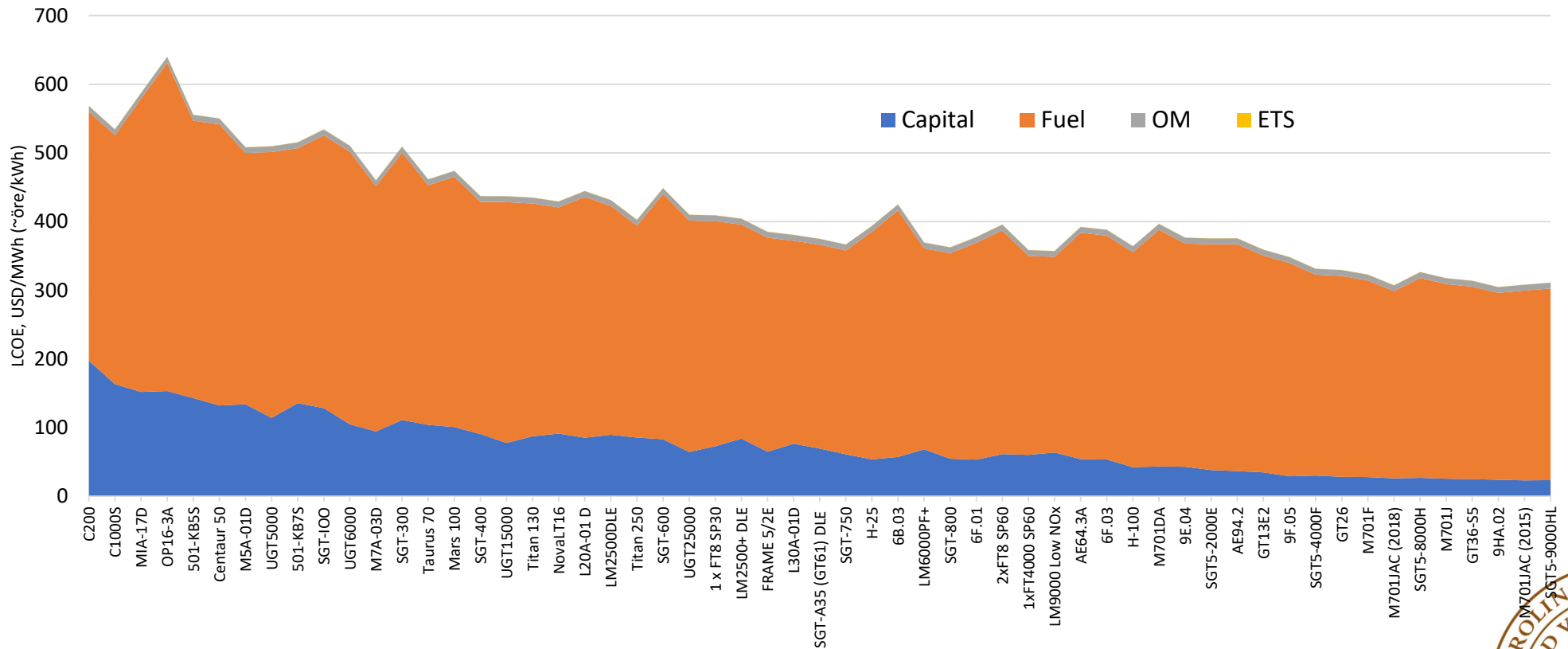
1000 h/a, 20 years, equity 0.4/0.08, and 0.6/0.04



Hydrogen @ 120 USD/MWh – a feasible solution?



Levelized Cost of Electricity



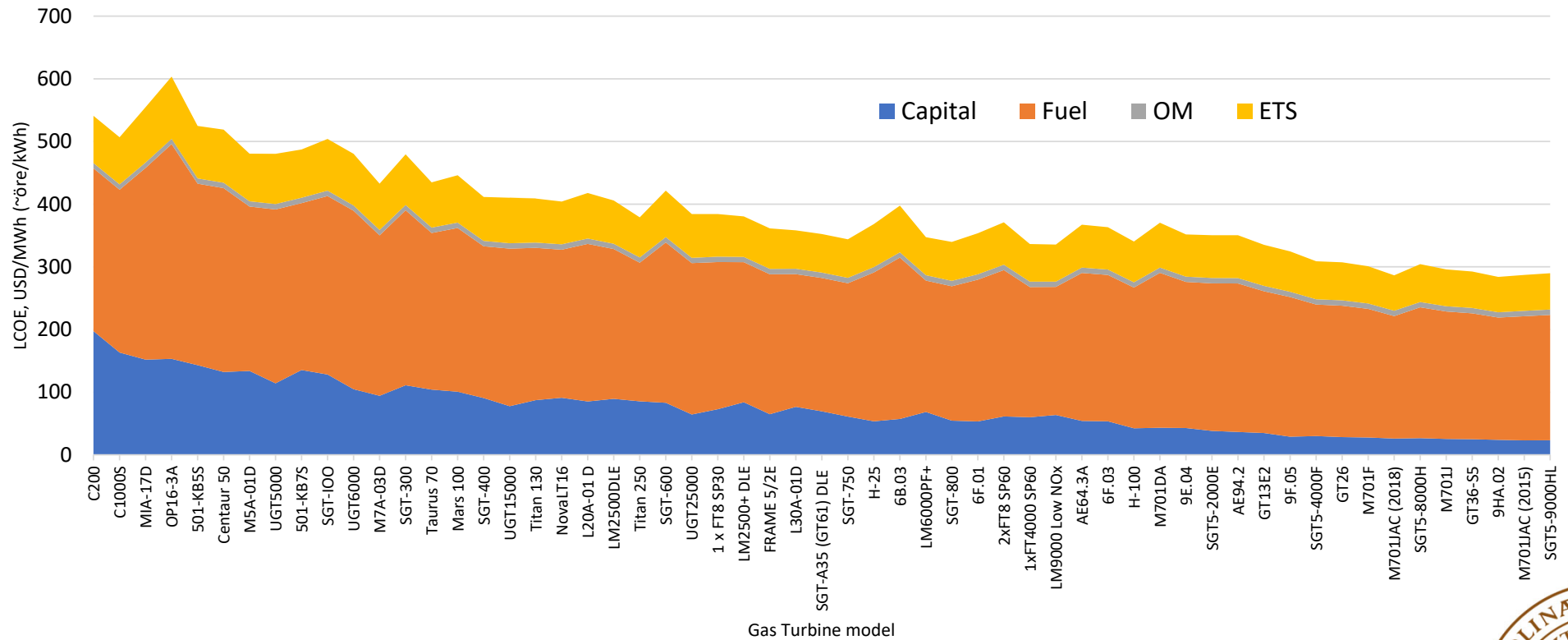
1000 h/a, 20 years, equity 0.4/0.08, and 0.6/0.04 Gas Turbine model



Methanol @ 86 USD/MWh – a convenient solution?



Levelized Cost of Electricity



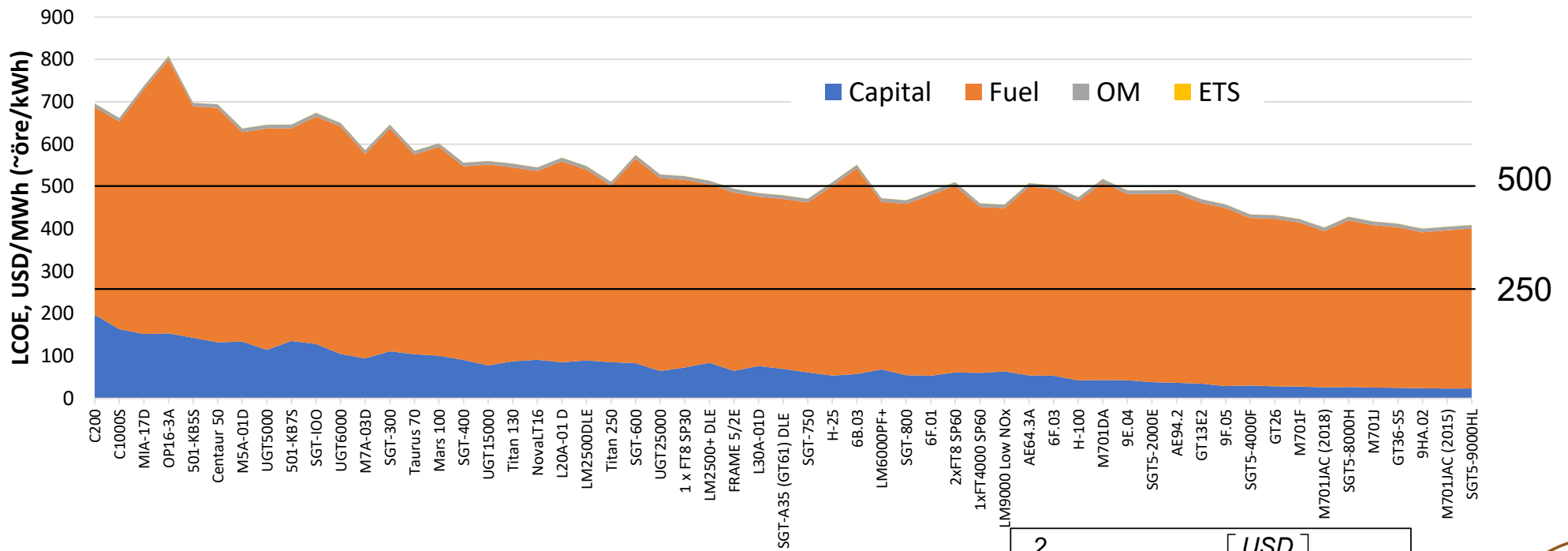
1000 h/a, 20 years, equity 0.4/0.08, and 0.6/0.04



HVO @ 162.2 USD/MWh – a feasible solution?



Levelized Cost of Electricity



1000 h/a, 20 years, equity 0.4/0.08, and 0.6/0.04

$$\frac{2}{44.4} \cdot 3600 \approx 162.2 \left[\frac{\text{USD}}{\text{MWh}} \right]$$

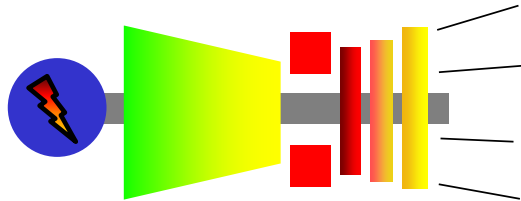
$$\therefore @40\%: \frac{162.2 \cdot 5}{2} \approx 406.25 \left[\frac{\text{USD}}{\text{MWh}} \right]$$



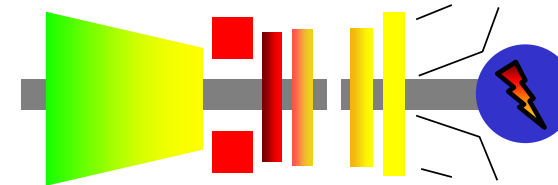
Gas turbine technology – some features!



Single- vs. multi-shaft industrial I



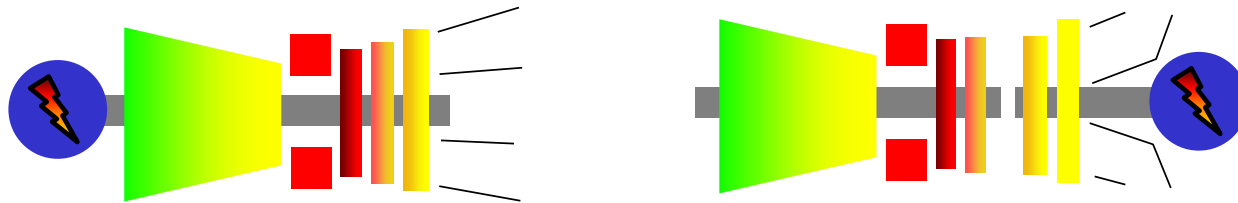
- Only power generation (torque issues)
- Part-load (pro's and con's) – effective way of controlling engine flow for high/constant exhaust temperature
- Exhaust size limitations (lower speed or high outlet velocity)
- Efficient exhaust
- 50/60 Hz direct drive for large units
- Beam rotor with two bearings



- Both power and driver
- Part-load (pros and cons)
- Lower starter power
- “Free” power turbine speed (lower outlet velocity level)
- Typically less efficient exhaust (lower recovery levels)
- Three-shaft aero-derivatives
- Low inertia (1...3 seconds)!
- PT over-speed risk at load rejection



Single- vs. multi-shaft industrial II



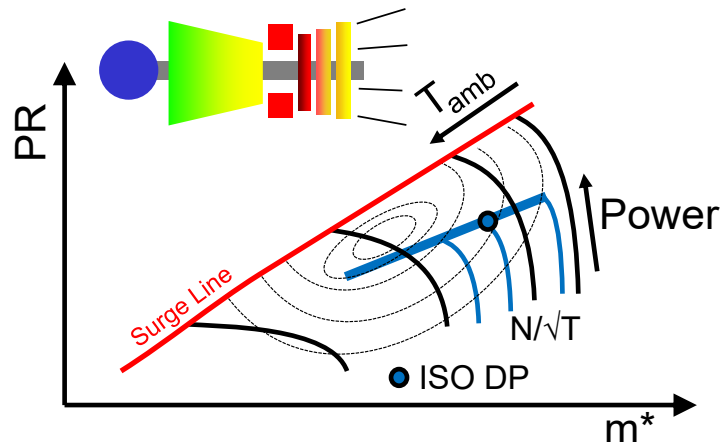
$$\underbrace{P_{Starter}}_{(A)} + \underbrace{P_{Turbine}}_{(B)} + \underbrace{\Delta P \cdot I}_{(C)} - \underbrace{P_{Compressor}}_{(D)} \geq 0$$

Where:

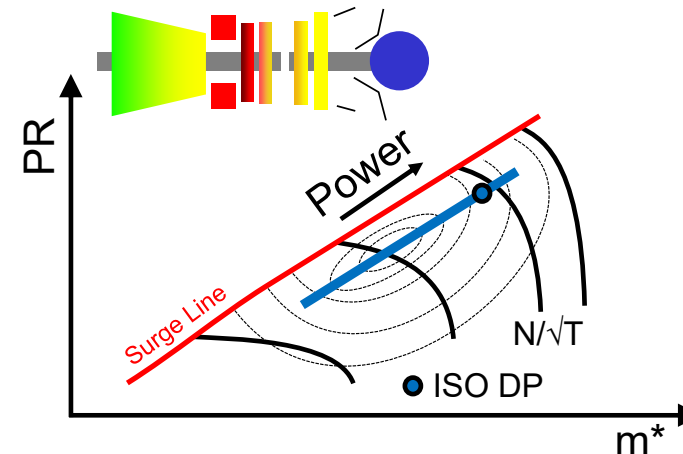
- (a) Starter power
- (b) Power delivered by the turbine
- (c) Power required for the defined acceleration
- (d) Power absorbed by the compressor



Single- vs. multi-shaft industrial III



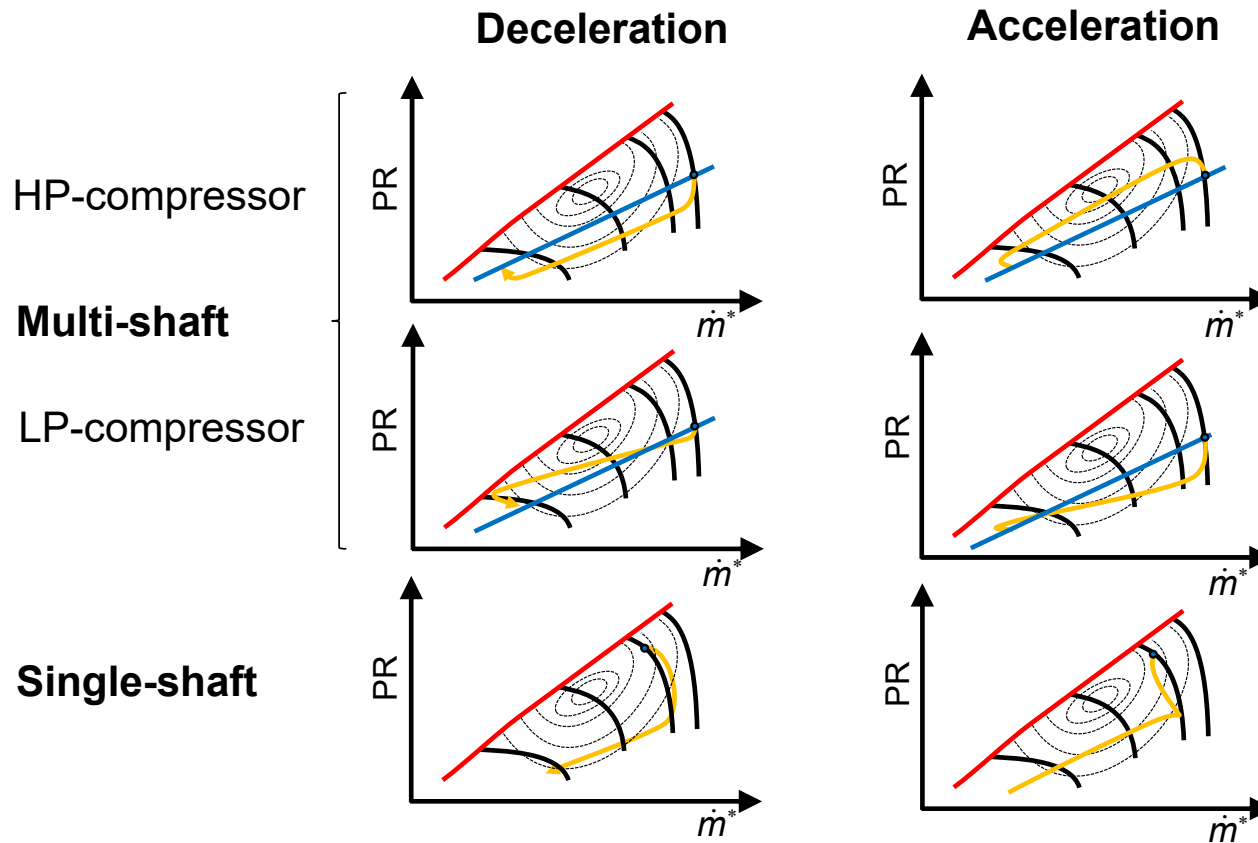
- Physical speed set by grid and gear ratio (<100 MW)
- Locus of operation at different ambient temp's with nominal firing could be seen as a "running line"
- No rotor inertia lag (frequency response)
- Typically reduced surge margin at high ambient temperatures (COT/T_1)
- Grid code requirement of 6% under-speed at $+50^\circ\text{C}$ – may be problematic!



- Typical speed range 60...105 %
- Compressor speed is decoupled from the load
- The running line is, more or less, a function of firing – not ambient temp – for a certain engine
- No real grid code issues except for inertia requirements ☺



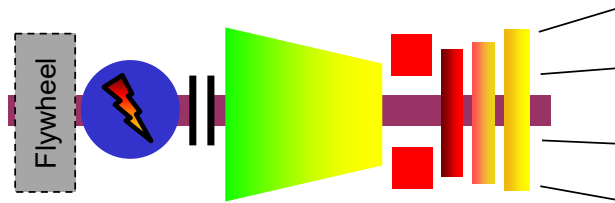
Single- vs. multi-shaft industrial IV



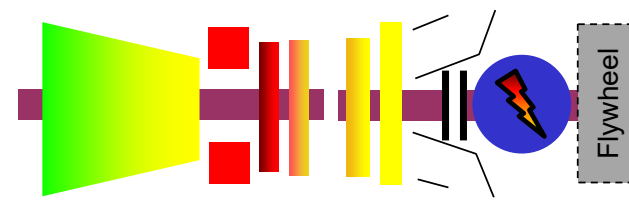
Synchronous condensation



Single-shaft with SSS-clutch

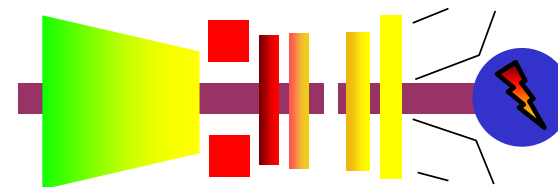


Twin-shaft with SSS-clutch



- Synchronous condensation without firing
 - ✓ Spinning PT?
 - ✓ SSS-clutch
 - ✓ Faster starts and less starter power
- Massive flywheel for increased inertia?
 - ✓ Inertia in a future grid with non-rotating turbines (< 4 m/s wind speed)?
- Power absorption
 - ✓ Single shaft compressor issues?
 - ✓ Gearbox (forcing)

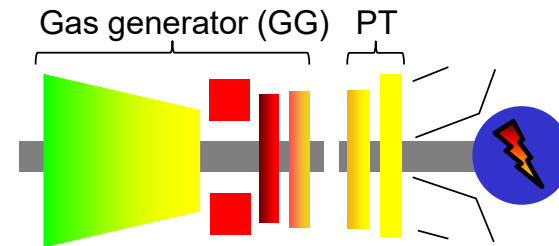
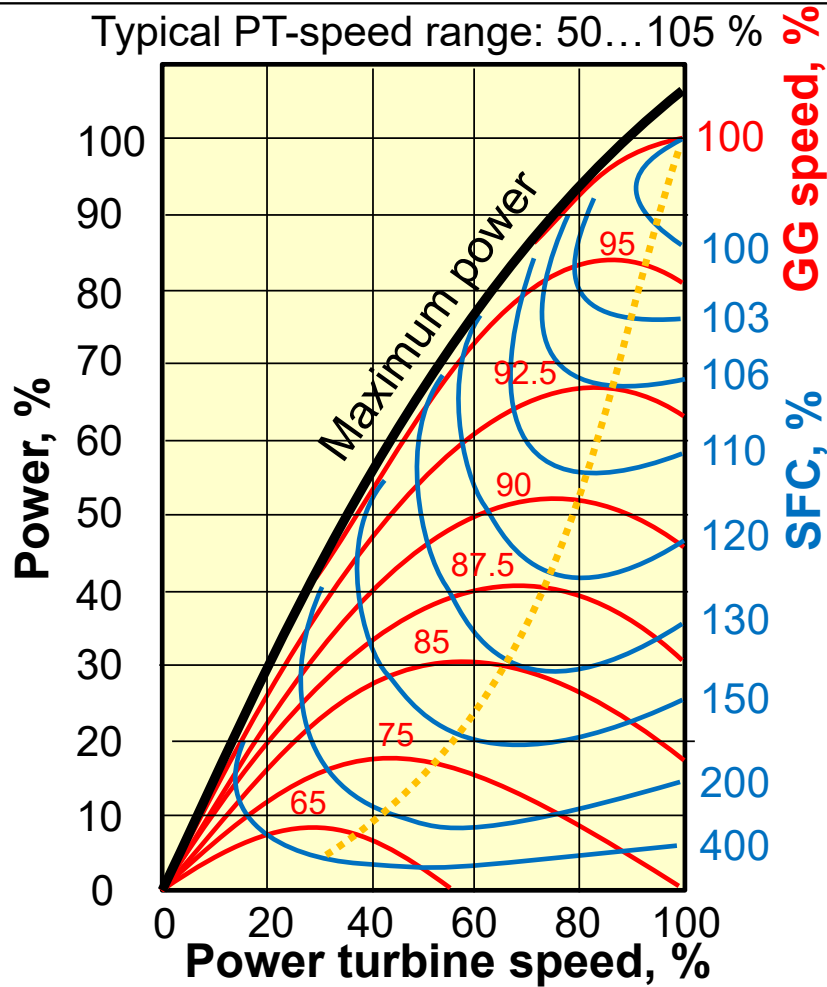
Twin-shaft with spinning PT



- Spinning PT – fast start
- 600...900 kW windage, i.e. **only non-geared PT's** (heat ~ speed³)



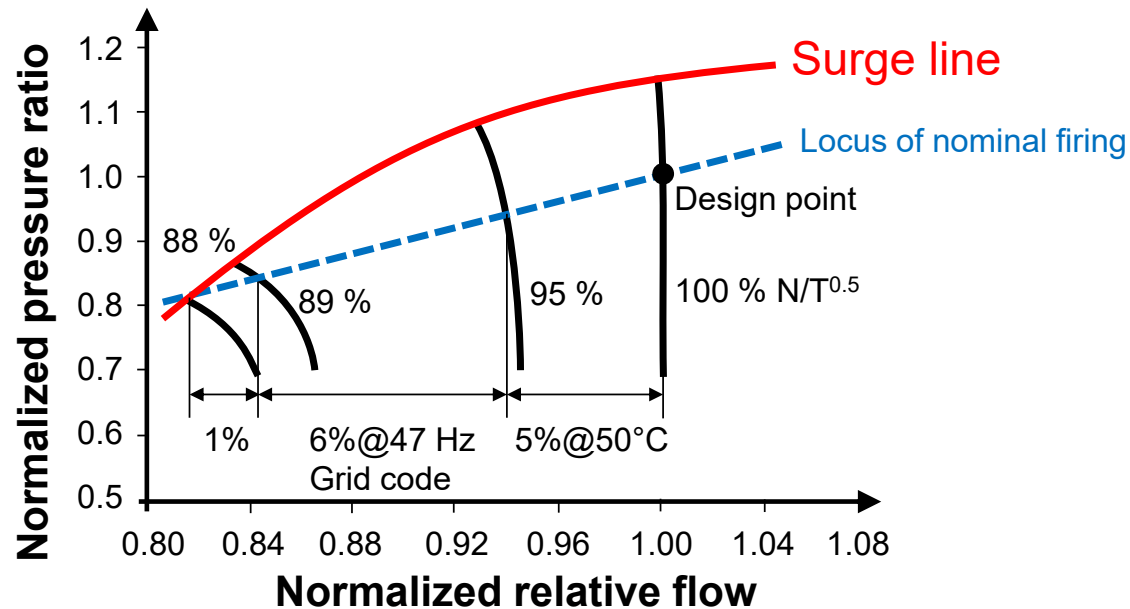
Power vs. PT- and GG speed



- No direct coupling between load speed and the compressor!
- Part-load (pros and cons)
- Lower starter power
- Slower than single-shaft units because of GG-lag
- Low inertia! (~1 s)
- PT over-speed risk at load rejection
- Break-away torque is typically twice the full load torque



Compressor and grid code...

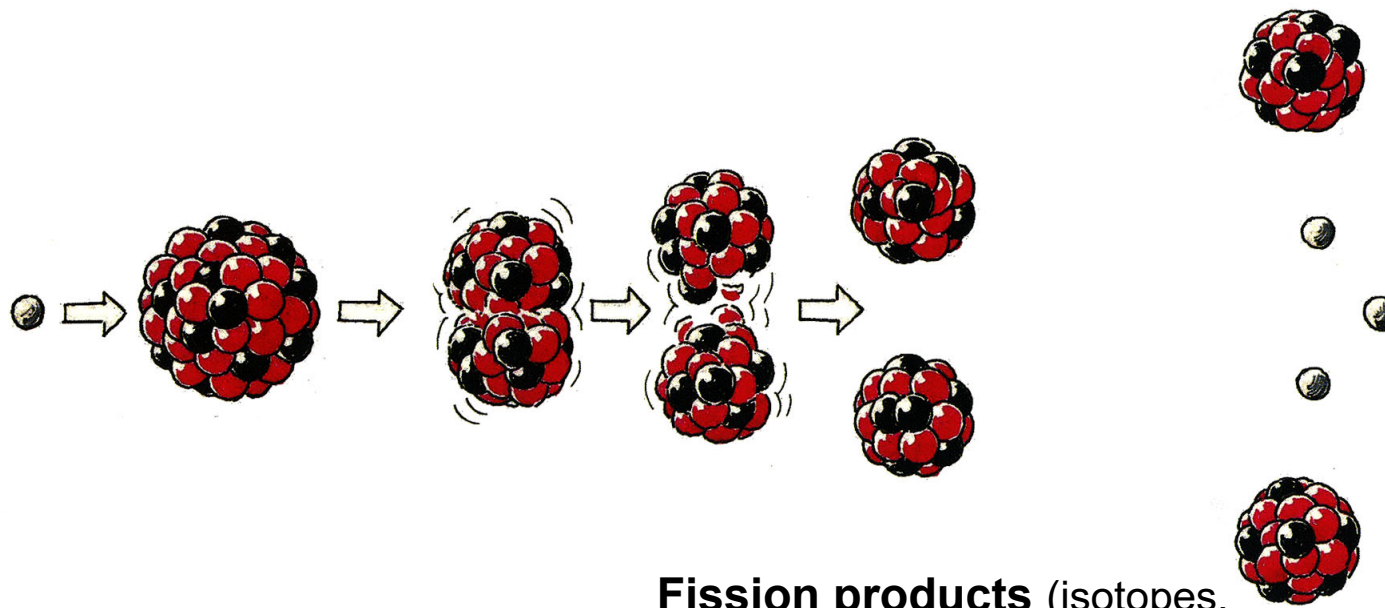


- Grid code requires only speed (47 Hz) and temperature variation
- Fouling has to be taken into consideration
- The load shall be nominal down to 49.5 Hz and then “pro rata” with frequency (hence over-firing or extra IGV) down to 47 Hz (UK)

Based on Wolfgang Kappis, "Compressors in Gas Turbine Systems, in "Modern Gas Turbine Systems"



NPP's



Fission products (isotopes,
e.g., Barium-141, Krypton-92)



NPP Cycle selection – fundamentals

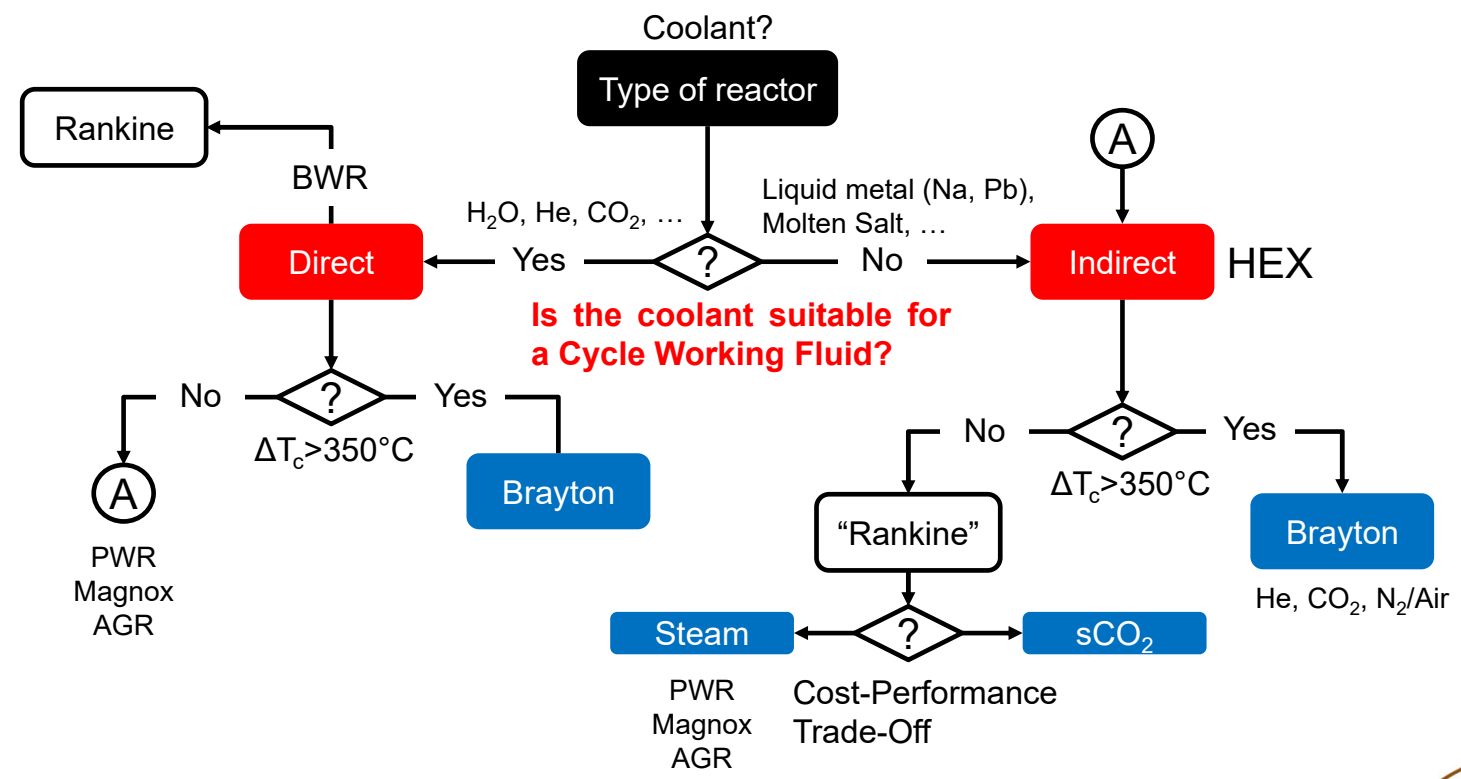


The material presented here is largely based on Dr Gülen

$$\eta_{th} \sim 1 - \frac{\bar{T}_{out}}{\bar{T}_{in}}$$

$$\bar{T}_{in} = \frac{\dot{Q}_{in}}{\int \frac{d\dot{Q}_{in}}{T}} = \frac{h_3 - h_2}{s_3 - s_2} = \frac{T_3 - T_2}{\ln(T_3/T_2)} \Big|_{c_p, p}$$

$$\bar{T}_{out} = \frac{T_4 - T_1}{\ln(T_4/T_1)} \Big|_{c_p, p}$$

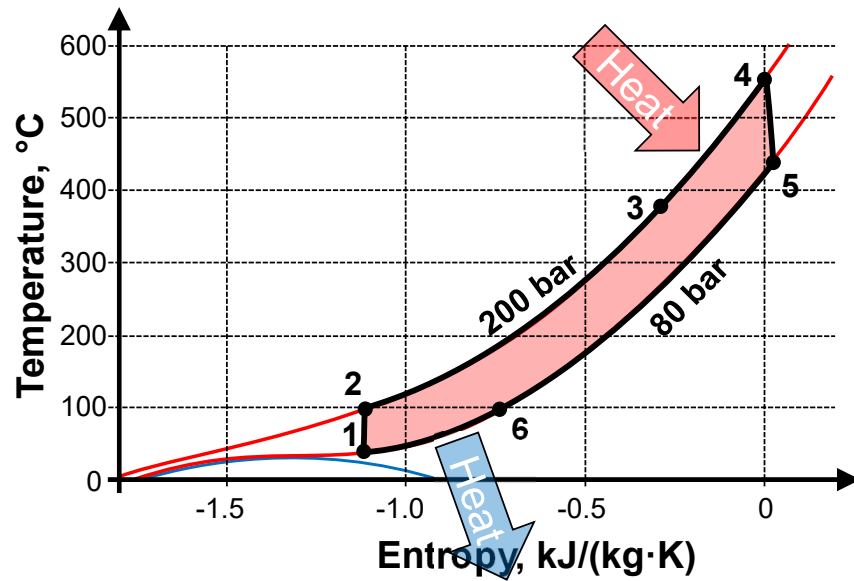


Super-critical CO₂-cycle (sCO₂)

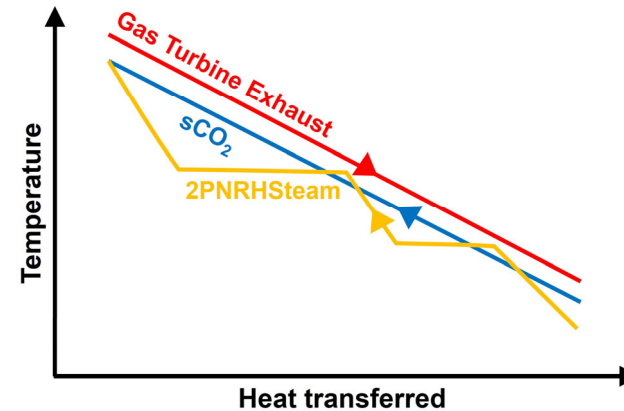
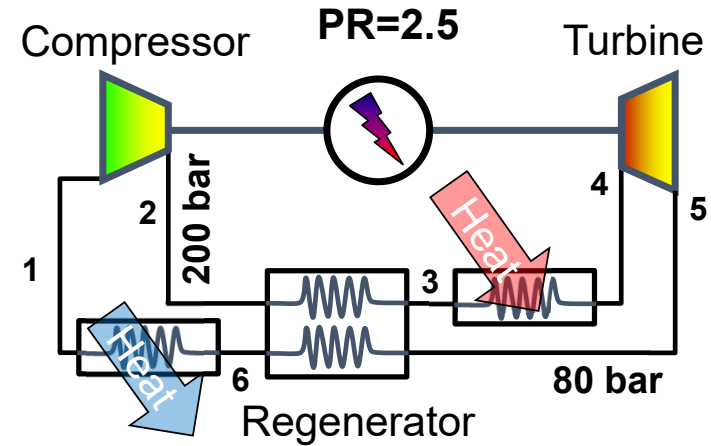


$$\dot{Q} = \dot{m} \cdot (h_3 - h_2) = \dot{m} \cdot (h_5 - h_6)$$

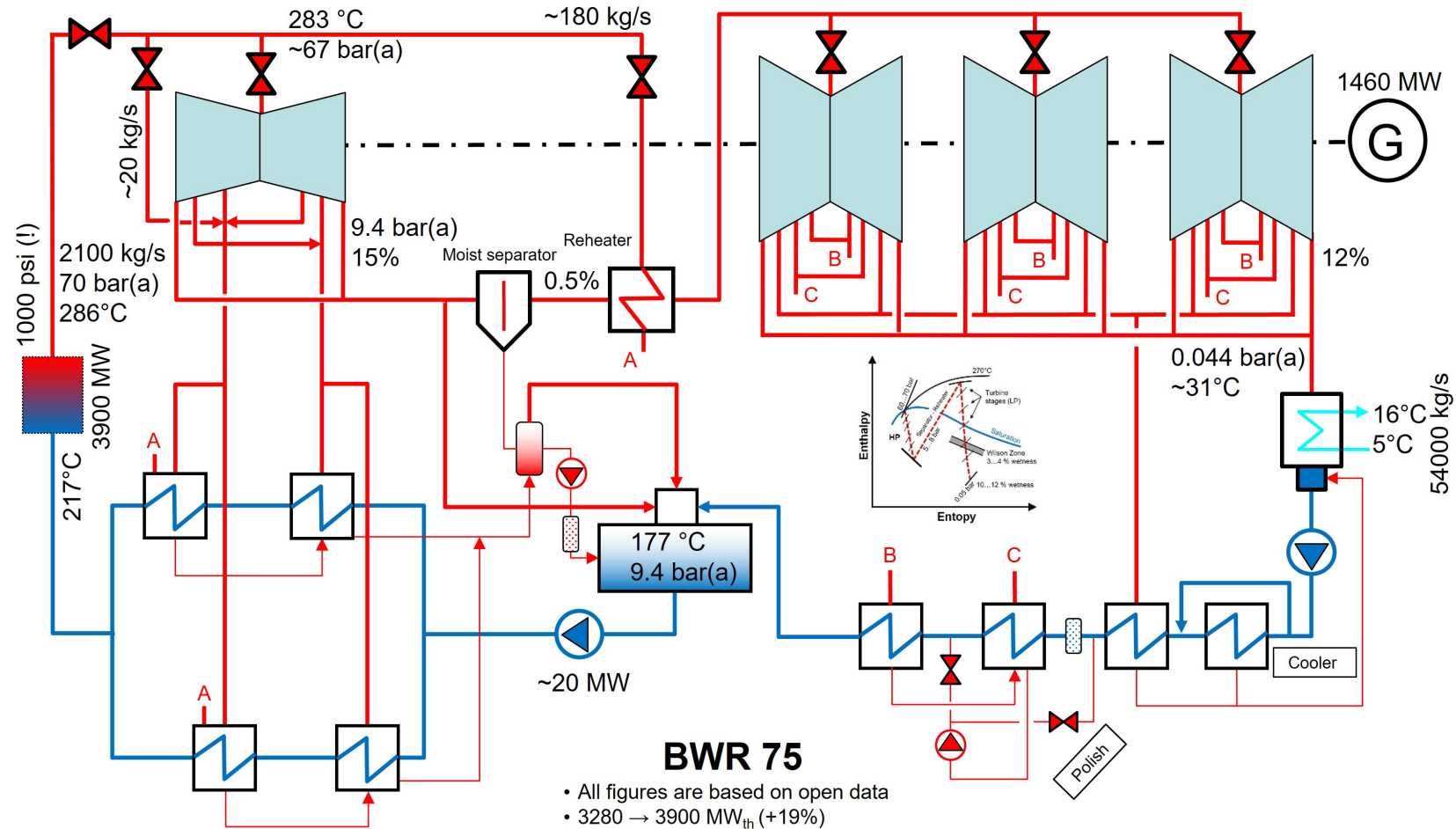
$$\varepsilon_{HX} \cong \frac{T_3 - T_2}{T_5 - T_6}$$



- Critical pressure = 73.773 bar(a)
- Recompression cycle for optimum performance (e.g. 42 → 50 percent efficiency @ 700°C/37°C)



Typical late 2nd generation BWR cycle



Stage efficiency level – Traupel 1977

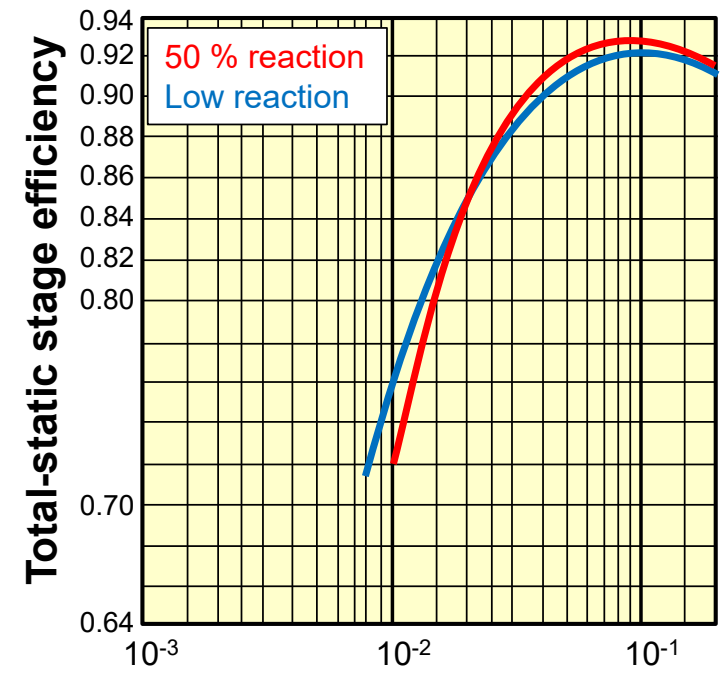
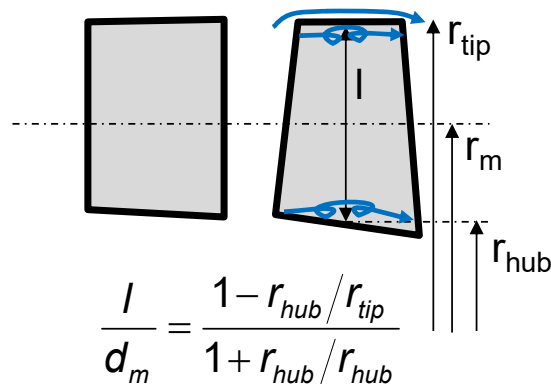


$$A = \pi \cdot (r_{tip}^2 - r_{hub}^2) = \pi \cdot \frac{2 \cdot (r_{tip} + r_{hub})}{2} \cdot (r_{tip} - r_{hub}) \dot{Q} = \pi \cdot d_m \cdot l \cdot \bar{c}_a = \pi \cdot l / d_m \cdot d_m^2 \cdot \bar{c}_a$$

$$\left. \begin{aligned} l/d_m \cdot \frac{\bar{c}_a}{u} &= \frac{1}{\pi} \cdot \frac{\dot{Q}}{d_m^2 \cdot u} \\ u &= \omega \cdot r_m \end{aligned} \right\} \therefore l/d_m \cdot \frac{\bar{c}_a}{u} = \frac{4}{\pi} \cdot \frac{\dot{Q} \cdot \omega^2}{u^3}$$

$$\left. \begin{aligned} l/d_m \cdot \frac{\bar{c}_a}{u} &= \frac{4}{\pi} \cdot \frac{\dot{Q} \cdot \omega^2}{u^3} \\ u &= \sqrt{\Delta h_s / k} \end{aligned} \right\} \therefore l/d_m \cdot \frac{\bar{c}_a}{u} = \frac{4 \cdot k^{3/2}}{\pi} \cdot \frac{\dot{Q} \cdot \omega^2}{\Delta h_s^{3/2}} = \frac{k^{3/2}}{\pi} \cdot q$$

$$\left. \begin{aligned} q &= \frac{\dot{Q} \cdot \omega^2}{\Delta h_s^{3/2}} \\ n_s &= \frac{\omega \cdot \dot{Q}^{1/2}}{\Delta h_s^{3/4}} \end{aligned} \right\} \therefore q = n_s^2$$



Based on: Traupel – Thermische Turbomaschinen, Band I, 1977, Fig. 9.5.4

$$\varepsilon \cdot \frac{c_a}{u} \cdot \frac{l}{d_m} = const \cdot \frac{\dot{Q} \cdot \omega^2}{\Delta h_s^{3/2}} = const \cdot n_s^2$$





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